Modeling and Simulation of Chemical System Vaporization at High Temperature: Application to the Vitrification of Fly Ashes and Radioactive Wastes by Thermal Plasma

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1. Introduction

The treatment, at high temperatures, of such chemical systems as the fly ashes and radioactive wastes requires the control of its element volatility. Precisely, it requires following the evolution of the system during treatment and determining the composition of the system in all phases.

For a closed chemical system, the calculation of its composition is carried out by the method of free enthalpy minimization developed by Eriksson [1]. However, for open systems, the problem is not definitively solved yet. A computer code simulating the volatility of the elements present in an oxide system was developed by Pichelin [2] and Badie [3]. This computer code was modified by Ghiloufi to control the vaporization of the elements present in a chloride and oxide system during the fly ashes vitrification by plasma and to study the radioelement volatility during the treatment of radioactive wastes by thermal plasma [4-9].

In this chapter we present a method used in our computer code, which is developed to simulate and to modulate a chemical system vaporization at high temperature. This method is based on the calculation of composition by free energy minimization of the system, coupled with the mass transfer equation at the reactional interface. This coupling is ensured by fixing the equivalent partial pressure of oxygen in the mass transfer equation and those characterizing the complex balances.

This chapter contains five parts: In the first part we will present the method used to the calculation of composition by free energy minimization of a closed system, precisely we will develop the equations characterizing the complex balances at the reactional interface. In the second part we will give the mass transfer equation of oxygen. In the third part we will present the method used in our study to determine the diffusion coefficients of gas species essentially for complex molecules like vapor metals. In the fourth part we will apply the computer code to simulate the radioelement volatility during the vitrification of radioactive wastes by thermal plasma. In the last part we will present the results obtained by the computer code during the study of radioelement volatility.
2. Description of the model

In the model, the species distribution in the liquid and gas phases is obtained iteratively using the calculation of system composition coupled with the mass transfer equation. The quantity of matter formed in the gas phase is distributed into three parts: The first part is in equilibrium with the bath, the second part is diffused in the diffusion layer, and the third part is retained by the bath under the electrolysis effects (Figure 1). The gas composition at the surface is thus modified. It is not the result of a single equilibrium liquid-gas, but instead, it is the outcome of a dynamic balance comprising: a combined action of reactional balances, electrolysis effects, and diffusive transport.

The flux density of a gas species $i$ ($J_i^L$) lost in each iteration is given by:

$$J_i^L = J_i^D - J_i^R$$

Where $J_i^D$ and $J_i^R$ are, respectively, the diffusion flux density and the flux retained by the bath for the gas species $i$.

The vaporization model is applicable to several types of complex chemical systems. It is independent of the geometrical configuration of the vaporization system, but it is developed based on the following three hypotheses:

a. The chemical system consists of two phases: a vapor phase, whose species are regarded as perfect gases, and a homogeneous isothermal liquid phase.

b. The model is mono-dimensional: it does not introduce discretization on the variable space, but enables to calculate the composition of the two phases at each time interval.

c. The mass transfer at the interface is controlled by the gas species diffusion in the carrier gas because the reaction kinetics at the liquid/gas interface are very fast.

Fig. 1. Simplified diagram used to establish the assumptions of the model
3. Calculation of the gas/liquid system composition

The free energy of a system made up of two phases; a vapor phase formed by \( M_l(1) \) species and a condensed phase consisting of \( M_l(2) \) species is as follows:

\[
G = \sum_{i=1}^{M_l(1)} n_i \left( g_i^0 + RT \log p_i \right) + \sum_{i=M_l(1)+1}^{M_l(1)+M_l(2)} n_i \left( g_i^0 + RT \log X_i \right)
\]  

where \( g_i^0 \) is the formation free enthalpy of a species under standard conditions, \( R \) is the perfect gas constant, \( T \) is the temperature, and \( n_i \) is the mole number of species \( i \). The two terms \( p_i \) and \( X_i \) are, respectively, the partial pressure of a gas species, assumed a perfect gas, and the molar fraction of species \( i \) in the liquid phase assumed ideal.

Equation (2) can be written differently as:

\[
F = \frac{G}{RT} = \sum_{i=1}^{M_l(1)} n_i \left[ \frac{g_i^0}{RT} + \log P + \log \frac{n_i}{n_g} \right] + \sum_{i=M_l(1)+1}^{M_l(1)+M_l(2)} n_i \left[ \frac{g_i^0}{RT} + \log \frac{n_i}{n_l} \right]
\]  

where \( P \) is the total pressure, \( n_g \) represents the total mole number of the species in the gas phase (\( n_g = \sum_{i=1}^{M_l(1)} n_i \)) and \( n_l \) represents the total mole number of the species in the condensed phase (\( n_l = \sum_{i=M_l(1)+1}^{M_l(1)+M_l(2)} n_i \)).

Let us assume that the system under study consists of \( L \) basic elements. Hence, the conservation of the elements mass results in:

\[
\sum_{i=1}^{M_l(1)} a_{ij} n_i + \sum_{i=M_l(1)+1}^{M_l(1)+M_l(2)} a_{ij} n_i = B_j \quad j \in [1, L]
\]  

where \( a_{ij} \) is the atoms grams number of the element \( j \) in the chemical species \( i \) and \( B_j \) is the total number of atoms grams of the element \( j \) in the system.

The equivalent partial pressure of oxygen is given by:

\[
P_{O2} = \frac{n_{O2}}{n_g} P
\]  

where \( n_{O2} \), representing the equivalent mole number of oxygen, is given by:

\[
n_{O2} = \sum_{i=1}^{M_l(1)} a_{iL} n_i
\]  

where \( a_{iL} \) is the atoms grams number of oxygen in the chemical species \( i \). Combining (5) and (6) leads to:
The calculation of the system composition to the balance coupled with the mass transfer equation, at constant temperature $T$ and constant pressure $P$, consists of minimizing the function $F$ under the constraints of (4) and (7). The Lagrange function becomes:

$$
L(n_i) = \xi(n_i) + \sum_{j=1}^{L} \Pi_j \left( - \sum_{i=1}^{Ml(1)+Ml(2)} a_{i} n_i + B_j \right) + \Pi_{L+1} \left( - \sum_{i=1}^{Ml(1)} a_{iL} n_i + \frac{P_{O2}}{P} n_g \right)
$$

where $\Pi_j$ represents the Lagrange multipliers and the function $\xi(n_i)$ is the Taylor series expansion of $F$ (with orders higher than two being neglected).

To minimize $F(n_i)$ subject to (4) and (7), it is required to have:

$$
\frac{\partial L}{\partial n_i} = 0 \quad i=1,\ldots,Ml(1)+Ml(2)
$$

$$
\frac{\partial L}{\partial \Pi_j} = 0 \quad j=1,\ldots,L, L+1
$$

From (9), the expression of the mole number of a species $i$ in the vapor phase or in the liquid phase can be deduced. That is to say:

For gases:

$$
n_i = \left( \frac{\xi_i^0}{RT} - \log P - \frac{\xi_i^0}{n_g^0 n_i^0} \right) + \frac{n_i^0}{n_g^0} + \sum_{j=1}^{L} \Pi_j a_{ij} + \Pi_{L+1} \left( a_{iL} - \frac{P_{O2}}{P} \right) n_i^0
$$

For liquid:

$$
n_i = \left( \frac{\xi_i^0}{RT} - \frac{\xi_i^0}{n_i^0} \right) + \frac{n_i^0}{n_g^0} + \sum_{j=1}^{L} \Pi_j a_{ij} n_i^0
$$

with $n_g^0 = \sum_{i=1}^{Ml(1)} n_i^0$ and $n_l^0 = \sum_{i=Ml(1)+1}^{Ml(1)+Ml(2)} n_i^0$

Substituting (11) and (12) in (10) results in a system of $L+3$ equations, whose unknown factors are the Lagrange multipliers ($\Pi_1$, $\Pi_2$, ..., $\Pi_L$, $\Pi_{L+1}$), $u_1$, and $u_2$.

with $u_1 = \frac{n_g^-}{n_g^0} - 1$ and $u_2 = \frac{n_l^-}{n_l^0} - 1$.

Solving this set of equations then using (11) or (12), as needed, gives the values of $n_i$. These values $n_i$ represent the improved values over the first iterations $n_i^{(1)}$. A loop of iterations is thus defined by using $n_i^{(k)}$ in the place of the $n_i^{(k-1)}$ for the $k^{th}$ iteration.
4. Transfer equation

4.1 Determination of the stoichiometric coefficient
To simplify the writing and calculation of the mass transfer equation at the interface, a dimensionless quantity $X_j$, called stoichiometric coefficient of a metal $J'$, has been introduced and corresponding to:

$$X_j = \frac{n_{O-J}}{n_{M_j}}$$  \hspace{1cm} (13)

where $n_{O-J}$ is the mole number of oxygen in the liquid phase related to metal $J'$, whereas the term $n_{M_j}$ represents the total mole number of metal $J'$ in the liquid phase, which contains m species. For example if N is the total mole number of metals in the mixing melted material, for an unspecified metal $J'$, the expressions of $X_j$ is as follows:

$$X_j = \frac{\sum_{i=1}^{m} a_{ik} n_i a_{ij} v_{ij}}{\sum_{i=1}^{m} a_{ij} n_i}$$  \hspace{1cm} (14)

$a_{ij}$ and $a_{ik}$ are respectively the stoichiometric coefficients of the element $J'$, and oxygen in species ‘$i$’. $n_i$ represents the number of moles of species ‘$i$’. $v_{ij}$ is the valence of metal $J'$ in oxide ‘$i$’.

4.2 Example
In an initial mixture of Al-Si-Fe-O-Cl, for example, the species which can exist in the liquid phase at 1700 K are as follows: SiO$_2$, Fe$_2$SiO$_4$, Fe$_3$O$_4$, FeO, Al$_2$O$_3$, AlCl$_3$, FeCl$_2$. The iron stoichiometric coefficients $X_{Fe}$ in the system is given by the following expression:

$$X_{Fe} = \frac{(4 n_{Fe_2SiO_4} \times \frac{4}{8}) + 4 n_{FeO} + n_{FeO}}{2 n_{Fe_2SiO_4} + 3 n_{Fe_3O_4} + n_{FeO}}$$  \hspace{1cm} (15)

4.3 Transfer equation
From equation (13), the oxygen mole number in the liquid phase related to metal $J'$, can be deduced, i.e.

$$n_{O-J} = X_j n_{M_j}$$  \hspace{1cm} (16)

If equation (16) is differentiated relatively to time and each term is divided by the surface of the interface value $A$, it comes:

$$\frac{1}{A} \frac{dn_{O-J}}{dt} = -\frac{1}{A} X_j \frac{dn_{M_j}}{dt} - \frac{1}{A} n_{M_j} \frac{dX_j}{dt}$$  \hspace{1cm} (17)
The interfacial density of molar flux of a species ‘i’ is:

\[ J_i = -\frac{1}{A} \frac{dn_i}{dt} \text{ (mole.s}^{-1}.\text{m}^{-2}) \] (18)

Introducing equation (18), in equation (17), leads to:

\[ (J_{O}^L)_{M_j} = X_j \cdot (J_{M_j}^L) - \frac{n_{M_j}}{A} \frac{dX_j}{dt} \] (19)

\( (J_{O}^L)_{M_j} \) represent the surfacic molar flux densities of oxygen related to metal ‘J’ from the liquid phase, whereas \( (J_{M_j}^L) \) is the equivalent density of molar flux of a metal J from the liquid phase.

The total surfacic densities of molar flux of oxygen from the liquid phase is expressed by:

\[ (J_{O}^L) = \sum_{j=1}^{N} (J_{O}^L)_{M_j} \] (20)

If in the equation (20) \( (J_{O}^L)_{M_j} \) is replaced by its expression given by the equation (19) it follows:

\[ (J_{O}^L) = \sum_{j=1}^{N} X_j (J_{M_j}^L) - \frac{1}{A} \sum_{j=1}^{N} n_{M_j} \frac{dX_j}{dt} \] (21)

Indicating by \( N_g \), the number of species which can exist in the vapor phase, the expressions of the total densities of molar flux of oxygen and an unspecified metal ‘J’ in gas phase are:

\[ (J_{O}^G) = \sum_{i=1}^{N_g} a_{ik} J^G_i \] (22)

\[ (J_{M_j}^G) = \sum_{i=1}^{N_g} a_{ij} J^G_i \] (23)

where \( J^G_i \) is the molar flux density of a gas species ‘i’.

The mass balance at the interfacial liquid to gas is expressed by the equality between the equivalent densities of molar flux of an element in the two phases, i.e.:

\[ (J_{i}^L) = (J_{i}^G) \] (24)

The use of matter conservation equations at the interface, for oxygen and metals, and the combination of equations (16), (17), (18), (19) and (20), lead to the following equation:

\[ \sum_{j=1}^{N} X_j (J_{M_j}^L) - \sum_{i=1}^{N_g} a_{ik} J^G_i - \frac{1}{A} \sum_{j=1}^{N} n_{M_j} \frac{dX_j}{dt} = 0 \] (25)
The equation (25) is the oxygen matter conservation equation or the transfer equation at the interface. Argon is used as a carrier gas. In the plasma conditions, it is supposed that argon is an inert gas, so its molar flux density is zero:

\[ J_{Ar}^{G} = 0 \]  

(26)

The density flux for a gas species ‘i’ is given by:

\[ J_{i}^{G} = -\frac{D_{i}}{RT}(p_{i}^{T} - p_{i}^{w}) + J_{T} \cdot p_{i}^{w} \]  

(27)

where \( p_{i}^{T} \) and \( p_{i}^{w} \) represent the interfacial partial pressure and the partial pressure in the carrier gas of species ‘i’ respectively; \( J_{T} \) is the total mass flux density with \( J_{T} = \sum_{i=1}^{n-1} J_{i}^{G} \), \( J_{Ar}^{G} = 0 \) and \( \sum_{i=1}^{n} p_{i}^{w} = 1\text{atm} \), \( \delta_{i} \) is boundary layer thickness, and \( D_{i} \) is diffusion coefficient.

5. Flux retained by the bath

The Faraday’s first law of electrolysis states that the mass of a substance produced at an electrode during electrolysis is proportional to the mole number of electrons (the quantity of electricity) transferred at that electrode [10]:

\[ m = \frac{Q \cdot M}{q \cdot v \cdot N_{A}} \]  

(28)

where \( m \) is the mass of the substance produced at the electrode (in grams), \( Q \) is the total electric charge passing through the plasma (in coulombs), \( q \) is the electron charge, \( v \) is the valence number of the substance as an ion (electrons per ion), \( M \) is the molar mass of the substance (in grams per mole), and \( N_{A} \) is Avogadro’s number. If the mole number of a substance \( i \) is initially \( n_{i}^{0} \), its mole number produced at the electrode is:

\[ n_{i} = \frac{Q}{q \cdot v \cdot N_{A}} \cdot n_{i}^{0} \]  

(29)

The interfacial density of molar flux of a species ‘i’ is:

\[ J_{i} = \frac{1}{A} \frac{dn_{i}}{dt} \text{ (mole.s}^{-1}.\text{m}^{-2}) \]  

(30)

The density \( (J_{i}^{R}) \), of molar flux of a species \( i \) retained by the bath under the electrolyses effects, can be obtained by substituting (29) in (30) to yield:

\[ J_{i}^{R} = \frac{1}{A} \frac{dn_{i}}{dt} = \frac{1}{A} \left( \frac{d}{dt} \left( \frac{Q}{q \cdot v \cdot N_{A}} \cdot n_{i}^{0} \right) \right) = \frac{n_{i}^{0}}{\Lambda \cdot q \cdot N_{A} \cdot v} \cdot \frac{dQ}{dt} \]  

(31)
\[ \frac{dQ}{dt} = I \] represents the current in the plasma and \( F = qN_A = 96485 \text{C.mol}^{-1} \) is Faraday’s constant. Equation (31) becomes:

\[ j_i^k = \frac{I}{A.F.\nu} n_i^0 \] (32)

6. Numerical solution

Newton’s numerical method solves the mass balance equations (26), (27) and (28) with respect to the interfacial thermodynamic equilibrium, the unknown parameters being the interfacial partial pressure \( P_i^w \), the stoichiometric coefficient \( X_j \) and the molar flux densities \( j_i^G \).

The convergence scheme is as follows:
- We calculate the liquid-gas interfacial chemical composition of the closed system by using Ericksson’s program. The oxygen partial pressure is then defined by the convergence algorithm.
- The recently known values of \( P_i^w \) and \( X_j \) are introduced into the mass equilibrium equations which can be solved after a series of iterative operations up to the algorithm convergence.
- At the beginning of the next vaporization stage, the system is restarted with the new data of chemical composition. The time increment is not constant and should be adjusted to the stage in order to prevent convergence instabilities when a sudden local variation of the mass flux density occurs.

7. Estimation of the diffusion coefficients

Up to temperatures of about 1000 K, the binary diffusion coefficients are known for current gases, oxygen, argon, nitrogen...etc. For temperatures higher than 1000 K, the diffusion coefficients of the gas species in the carrier gas are calculated according to level 1 of the CHAPMAN-ENSKOG approximation [11]:

\[ D_{ij} = 0.002628 \frac{\sqrt{T^3 (M_i + M_j) / 2M_i M_j}}{P \sigma_{ij}^2 \Omega_{ij}^{11}(T^*_ij)} \] (33)

In this equation \( D_{ij} \) is the binary diffusion coefficient (in cm\(^2\)s\(^{-1}\)), \( M_i \) and \( M_j \) are the molar masses of species ‘i’ and ‘j’. \( P \) is the total pressure (in atm), \( T \) is the temperature (in K), \( T^* = T \frac{k}{e_{ij}} \) is the reduced temperature, \( K \) is the Boltzmann constant, \( \sigma_{ij} \) is the collision diameter (in Å), \( e_{ij} \) is the binary collision energy and \( \Omega_{ij}^{11}(T^*_ij) \) is the reduced collision integral.

For an interaction between two non-polar particles ‘i’ and ‘j’:

\[ e_{ij} = \sqrt{e_i e_j} \] (34)
\[
\sigma_{ij} = \frac{1}{2} (\sigma_i + \sigma_j)
\]  

(35)

The values relating to current gases needed for our calculations are those of Hirschfelder [11]. For the other gas species, such as the metal vapor, the parameters of the intermolecular potential remain unknown whatever the interaction potential used. This makes impossible the determination of the reduced collision integral. For this reason the particles are regarded as rigid spheres and the collision integrals are assimilated to those obtained with the rigid spheres model [12]. That is equivalent to the assumption:

\[
\Omega_{ij}^{(1.1)^{\ast}} (T^*) = 1
\]  

(36)

\[
\sigma_{ij} = r_i + r_j
\]  

(37)

The terms \(r_i\) and \(r_j\) are the radii of the colliding particles. For the monoatomic particles, the atomic radii are already found. For the polyatomic particles, the radii of the complex molecules \(A_nB_m\) are unknown. Thus it has been supposed that they had a spherical form and their radii were estimated according to [12]:

\[
r_{A_nB_m} = \left| n r_A^3 + m r_B^3 \right|^{1/3}
\]  

(38)

In the above expression, \(r_A\) and \(r_B\) are either of the ionic radius, or of the covalence radius according to the existing binding types. The radii of all the ions which form metal oxides and chlorides are extracted from the Shannon tables [13].

At high temperature \((T > 1000\, \text{K})\), the \(D_i\) variation law with the temperature is close to the power 3/2 [14]. For this reason the diffusion coefficients of the gas species are calculated with only one value of temperature \((1700\, \text{K})\). For the other temperatures the following equation is applied:

\[
D_{ij}(T_2) = D_{ij}(T_1) \left( \frac{T_2}{T_1} \right)^{3/2}
\]  

(39)

8. Application of the model

To simulate the same emission spectroscopy conditions in which the experimental measurement are obtained, the containment matrix used for this study is formed by basalt, and its composition is given in table 1. At high temperatures \((T > 1700\, \text{K})\), in the presence of oxygen and argon, the following species are preserved in the model:

- In the vapor phase: \(\text{O}_2\), \(\text{O}\), \(\text{Mg}\), \(\text{MgO}\), \(\text{K}\), \(\text{KO}\), \(\text{Na}\), \(\text{Na}_2\), \(\text{NaO}\), \(\text{Ca}\), \(\text{CaO}\), \(\text{Si}\), \(\text{SiO}\), \(\text{SiO}_2\), \(\text{Al}\), \(\text{AlO}\), \(\text{AlO}_2\), \(\text{Fe}\), \(\text{FeO}\), \(\text{Ti}\), \(\text{TiO}\), \(\text{TiO}_2\), and \(\text{Ar}\).
- In the condensed phase: \(\text{CaSiO}_3\), \(\text{Ca}_2\text{SiO}_4\), \(\text{CaMgsi}_2\text{O}_6\), \(\text{K}_2\text{SiO}_3\), \(\text{SiO}_2\), \(\text{Fe}_2\text{SiO}_4\), \(\text{Fe}_3\text{O}_4\), \(\text{FeO}\), \(\text{FeNaO}_2\), \(\text{Al}_2\text{O}_3\), \(\text{CaO}\), \(\text{Na}_2\text{O}\), \(\text{Na}_2\text{SiO}_3\), \(\text{Na}_2\text{SiO}_5\), \(\text{K}_2\text{O}\), \(\text{K}_2\text{SiO}_3\), \(\text{MgO}\), \(\text{MgAl}_2\text{O}_4\), \(\text{MgSiO}_3\), \(\text{Mg}_2\text{SiO}_4\), \(\text{CaTiSiO}_5\), \(\text{MgTi}_2\text{O}_5\), \(\text{Mg}_2\text{TiO}_4\), \(\text{Na}_2\text{TiO}_5\), \(\text{Na}_2\text{Ti}_2\text{O}_7\), \(\text{TiO}\), \(\text{TiO}_2\), \(\text{Ti}_2\text{O}_3\), \(\text{Ti}_3\text{O}_5\), and \(\text{Ti}_4\text{O}_7\).
This study focuses on the three radioelements $^{137}$Cs, $^{60}$Co, and $^{106}$Ru. Ruthenium is a high activity radioelement, and it is an emitter of $\alpha$, $\beta$ and $\gamma$ radiations, with long a radioactive period. However, Cesium and Cobalt are two low activity radioelements and they are emitters of $\beta$ and $\gamma$ radiations with short-periods on the average (less than or equal to 30 years) [15]. To simplify the system, the radioelements are introduced separately in the containment matrix, in their most probable chemical form. Table 2 recapitulates the chemical forms and the mass percentages of the radioelements used in the system. The mass percentages chosen in this study are the same as that used in experimental measurements made by [9, 16].

<table>
<thead>
<tr>
<th>radioelement</th>
<th>$^{137}$Cs</th>
<th>$^{60}$Co</th>
<th>$^{106}$Ru</th>
</tr>
</thead>
<tbody>
<tr>
<td>Most probable chemical form</td>
<td>Cs$_2$O</td>
<td>CoO</td>
<td>Ru</td>
</tr>
<tr>
<td>% in mass</td>
<td>10</td>
<td>10</td>
<td>5</td>
</tr>
</tbody>
</table>

Table 2. Chemical Forms and Mass Percentages of radioelement

The addition of these elements to the containment matrix, in the presence of oxygen, leads to the formation of the following species:

- In the vapor phase: Cs, Cs$_2$, CsK, CsNa, CsO, Cs$_2$O, Cs$_2$O$_2$, Ru, RuO, RuO$_2$, RuO$_3$, RuO$_4$, Co, Co$_2$, and CoO.
- In the condensed phase: Cs, Cs$_2$O, Cs$_2$O$_2$, Cs$_2$SiO$_3$, Cs$_2$Si$_2$O$_5$, Cs$_2$Si$_4$O$_9$, Ru, CoAl, CoO, Co$_2$SiO$_4$, CoSi, CoSi$_2$, Co$_2$Si, and Co.

These species are selected with the assistance of the HSC computer code [17]. In the simulation, the selected formation free enthalpies of species are extracted from the tables of [18-20].

9. Simulation results

In this part we will present only the results of radioelement volatility obtained by our computer code during the treatment of radioactive wastes by plasma. However the results of heavy metal volatility during fly ashes treatment by thermal plasma can be find in [4,5].

9.1 Temperature influence

To have the same emission spectroscopy conditions in which the experimental measurement are obtained [9, 16], in this study the partial pressure of oxygen in the carrier gas $P_{O_2}$ is fixed at 0.01 atm, the total pressure $P$ at 1 atm, and the plasma current $I$ at 250 A. Figures 2 and 3 depict respectively, the influence of bath surface temperatures on the Cobalt and Ruthenium volatility. Up to temperatures of about 2000 K, Cobalt is not volatile. Beyond this
value, any increase of temperature causes a considerable increase in both the vaporization speed and the vaporized quantity of $^{60}$Co. This behavior was also observed for $^{137}$Cs [8]. Contrarily to Cobalt, Ruthenium has a different behavior with temperature. For temperatures less than 1700 K and beyond 2000 K, Ruthenium volatility increases with temperature increases. Whereas in the temperature interval between 1700 K and 2000 K, any increase of temperature decreases the $^{106}$Ru volatility.

To better understand this Ru behavior, it is necessary to know its composition at different temperatures. Table 3 presents the mole numbers of Ru components in the gas phase at different temperatures obtained from the simulation results.

<table>
<thead>
<tr>
<th>Mole numbers</th>
<th>species</th>
<th>Ru</th>
<th>RuO</th>
<th>RuO$_2$</th>
<th>RuO$_3$</th>
<th>RuO$_4$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1700K</td>
<td>6.10$^{-14}$</td>
<td>3.10$^{-10}$</td>
<td>4.10$^{-6}$</td>
<td>7.10$^{-5}$</td>
<td>1.10$^{-6}$</td>
<td></td>
</tr>
<tr>
<td>2000K</td>
<td>5.10$^{-11}$</td>
<td>2.10$^{-8}$</td>
<td>1.10$^{-5}$</td>
<td>3.10$^{-5}$</td>
<td>1.10$^{-7}$</td>
<td></td>
</tr>
<tr>
<td>2500K</td>
<td>1.10$^{-7}$</td>
<td>2.10$^{-6}$</td>
<td>8.10$^{-5}$</td>
<td>1.10$^{-5}$</td>
<td>2.10$^{-8}$</td>
<td></td>
</tr>
</tbody>
</table>

Table 3. Mole numbers of Ru components in the gas phase at different temperatures

Fig. 2. Influence of temperature on Co volatility

The first observation that can be made is that the mole numbers of Ru, RuO, and RuO$_2$ increase with temperature, contrary to RuO$_3$ and RuO$_4$ whose mole numbers decrease with increasing temperatures. These results are logical because the formation free enthalpies of Ru, RuO, and RuO$_2$ decrease with temperature. Therefore, these species become more stable when the temperature increases, while is not the case for RuO$_3$ and RuO$_4$. A more interesting observation is that at temperatures between 1700 and 2000 K the mole numbers of Ru, RuO, and RuO$_2$ increase by an amount smaller that the amount of decrease of the
mole numbers of $\text{RuO}_3$ and $\text{RuO}_4$ resulting in an overall reduction of the total mole numbers formed in the gas phase. At temperature between 2000 and 2500 K the opposite phenomenon occurs.

![Graph showing influence of temperature on Ru volatility](image)

Fig. 3. Influence of temperature on Ru volatility

### 9.2 Effect of the atmosphere

The furnace atmosphere is supposed to be constantly renewed with a composition similar to that of the carrier gas made up of the mixture argon/oxygen. For this study, the temperature is fixed at 2500 K, the total pressure $P$ at 1 atm and the plasma current $I$ at 250 A. Figures 4 and 5 present the results obtained for $^{60}\text{Co}$ and $^{106}\text{Ru}$ as a function of $P_{O_2}$.

For $^{60}\text{Co}$, a decrease in the vaporization speed and in the volatilized quantity can be noticed when the quantity of oxygen increases, i.e., when the atmosphere becomes more oxidizing. The presence of oxygen in the carrier gas supports the incorporation of Cobalt in the containment matrix. The same behavior is observed in the case of $^{137}\text{Cs}$ in accordance with $P_{O_2}$ [8].

When studying the Ruthenium volatility presented in the curves of figure 5 it is found that, contrary to $^{60}\text{Co}$, this volatility increases with the increase of the oxygen quantity. This difference in the Ruthenium behavior compared to Cobalt can be attributed to the redox character of the majority species in the condensed phase and gas in equilibrium. For $^{60}\text{Co}$, the oxidation degree of the gas species is smaller than or equal to that of the condensed phase species, hence the presence of oxygen in the carrier gas supports the volatility of $^{60}\text{Co}$. Whereas $^{106}\text{Ru}$, in the liquid phase, has only one form (Ru). Hence, the oxidation degree of the gas species is greater than or equal to that of liquid phase species and any addition of oxygen in the gas phase increases its volatility.
Fig. 4. Influence of the atmosphere nature on the Co volatility

Fig. 5. Influence of the atmosphere nature on the Ru volatility
9.3 Influence of current
To study the influence of the current on the radioelement volatility, the temperature and the partial pressure of oxygen are fixed, respectively, at 2200 K and at 0.2 atm, whereas the plasma current is varied from 0 A to 600 A. Figures 6 and 7 depict the influence of plasma

Fig. 6. Influence of plasma current on Co volatility

Fig. 7. Influence of current on Cs volatility
current on the Cobalt and Cesium volatility. The curves of these figures indicate that the increase of the plasma current considerably increases both the vaporization speed and the vaporized quantity of $^{60}$Co and $^{137}$Cs.

In the model, the electrolyses effects are represented by the ions flux retained by the bath, given by equation (32), which depends essentially on the plasma current. As the evaporation kinetics decrease with intensity current, the bath is in cathode polarization which prevents $^{60}$Co and $^{137}$Cs from leaving the liquid phase. These results assert the validity of equation (32) used by this computer code and conforms to the experimental results obtained by spectroscopy emission [9, 16]. The same behavior is observed in the case of $^{106}$Ru as a function of plasma current.

### 9.4 Influence of matrix composition

Three matrices are used in this study and their compositions are given in table 4. Matrix 1 is obtained by the elimination of 29 g of Silicon for each 100 g of basalt, whereas matrix 2 is obtained by the addition of 65 g of Silicon for each 100 g of basalt, and matrix 3 is basalt. Figures 8 and 9 depict the influence of containment matrix composition, respectively, on the Cobalt and Cesium volatility. The increase of silicon percentage in the containment matrix supports the incorporation of $^{60}$Co and $^{137}$Cs in the matrix.

For $^{137}$Cs, the increase of silicon percentage in the containment matrix is accompanied by an increase in mole numbers of $\text{Cs}_2\text{Si}_2\text{O}_5$ and $\text{Cs}_2\text{Si}_4\text{O}_9$ in the condensed phase. The presence of these two species in addition to $\text{Cs}_2\text{SiO}_3$ in significant amounts (between $10^{-3}$ and $10^{-2}$ mole) prevents Cs from leaving the liquid phase and reduces its volatility. For Cobalt, the increase of silicon percentage in the system supports the confinement of $^{60}$Co in the condensed phase in the $\text{Co}_2\text{SiO}_4$ form. Ruthenium is not considered in this study because, in the liquid phase, it has only the Ru form and any modification in the containment matrix has no effect on its volatility.

![Fig. 8. Influence of matrix composition on Co volatility](www.intechopen.com)
9.5 Distribution of Co and Ru on its elements during the treatment

Figures 10 and 11 depict the distribution of Cobalt components on the liquid and gas phases. In the gas phase, Cobalt exists essentially in the form of Co and, to a smaller degree, in the CoO form. In the liquid phase, Cobalt is found in quasi totality in CoO, Co and Co$_2$SiO$_4$ forms.

Figure 12 presents the distribution of Ruthenium components on the liquid and gas phases. In the gas phase, Ruthenium exists essentially in the form of RuO$_2$ and, to a smaller degree, in the form of RuO$_3$ and RuO, whereas Ru and RuO$_4$ exist in much smaller quantities compared to the other forms. In the liquid phase, Ruthenium has only the Ru form.
Fig. 11. Variation of the mole numbers of Co composition in the liquid phase

Fig. 12. Variation of the mole numbers of Ru composition in the gas and liquid phases
10. Comparison with the experimental results

The experimental setup is constituted of a cylindrical furnace, which supports a plasma device with twin-torch transferred arc system. The two plasma torches have opposite polarity. The reactor and the torches are cooled with water under pressure by two completely independent circuits. Argon is introduced at the tungsten cathode and the copper anode while oxygen, helium and hydrogen are injected through a water-cooled pipe [21]. To perform spectroscopic diagnostic above the molten surface, a water cooled stainless-steel crucible is placed under the coupling zone of the twin plasma torches. This crucible is filled with basalt and 10 % in oxide mass of Cs. On the cooled walls, the material does not melt and, hence, runs as a self-crucible. The intensities of the Ar line ($\lambda = 667.72$ nm) and the Cs line ($\lambda = 672.32$ nm) are measured by using an optical emission spectroscopy method (figure 13). The molar ratio Cs/Ar is deduced from the intensity ratio of the two lines [9, 16].

![Example of spectrum: Cs line ($\lambda = 672.32$ nm)](image)

Fig. 13. Schematic of the experimental setup: (1) reactor vessel; (2) cathode torch; (3) anode torch; (4) spherical-bearing arrangement; (5) injection lance; (6) crucible; (7) porthole; (8) optical system; (9) monochromator; (10) OMA detector; (11) computer.

Figure 14 shows the code results in comparison with the experimental measurements. This figure reveals that the experimental and simulation results are relatively close. The
small difference between the simulation results and the experimental measurements can be attributed to the measurements errors. In fact, the estimated error committed on the measurement of the ratio Cs/Ar is around 10% [9, 16]. The model calculations assumed a bath fully melted and homogeneous from the beginning (t = 0s), while in practice the inside of the crucible is not fully melted and there is a progress of fusion front that allows a permanent alimentation of the liquid phase in elements from the solid. These causes explain the perturbation of the experimental measurements and the large gap between these measurements and the results obtained by the model in the first few minutes.

![Graph](image.png)

Fig. 14. Comparison between the simulation and experimental results in the case of Cs

11. Conclusion

The objective of this method is to improve the evaporation phenomena related to the radioelement volatility and to examine their behavior when they are subjected to a heat treatment such as vitrification by arc plasma. The main results show that up to temperatures of about 2000 K, Cobalt is not volatile. For temperatures higher than 2000 K, any increase in molten bath temperature causes an increase in the Cobalt volatility. Ruthenium, however, has a different behavior with temperature compared to Cobalt. For temperatures less than 1700 K and beyond 2000 K, Ruthenium volatility increases when temperature increases. Whereas in the temperature interval from 1700 K to 2000 K, any increase of temperature decreases the Ru volatility. Oxygen flux in the carrier gas supports the radioelement incorporations in the containment matrix, except in the case of the Ruthenium which is more volatile under an oxidizing atmosphere. For electrolyses
effects, an increase in the plasma current considerably increases both the vaporization speed and the vaporized quantities of Cs and Co. The increase of silicon percentage in the containment matrix supports the incorporation of Co and Cs in the matrix. The comparison between the simulation results and the experimental measurements reveals the adequacy of the computer code.

12. Acknowledgements

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13. Nomenclature

\( J_i^D \): diffusion flux density for the gas species \( i \).

\( J_i^R \): flux retained by the bath for the gas species \( i \).

\( G \): free energy of a system.

\( g_i^0 \): formation free enthalpy of a species under standard conditions.

\( R \): perfect gas constant.

\( T \): temperature.

\( n_i \): mole number of species \( i \).

\( p_i \): partial pressure of a gas species.

\( X_i \): molar fraction of species \( i \) in the liquid phase.

\( P \): total pressure.

\( n_g \): total mole number of the species in the gas phase.

\( n_l \): total mole number of the species in the condensed phase.

\( a_i \): atoms grams number of the element \( j \) in the chemical species \( i \).

\( B_j \): total number of atoms grams of the element \( j \) in the system.

\( n_{O_2} \): equivalent mole number of oxygen.

\( L \): Lagrange function.

\( \Pi_j \): Lagrange multipliers.

\( \xi (n_i) \): Taylor series expansion of \( F \) (\( F=G/RT \)).

\( n_{O_j} \): mole number of oxygen in the liquid phase related to metal \( 'J' \).

\( n_{M_j} \): total mole number of metal \( 'J' \) in the liquid phase.

\( v_{ij} \): valence of metal \( 'J' \) in oxide \( 'i' \).

\( A \): value of interface surface.

\( J_i \): interfacial density of molar flux of a species \( 'i' \).

\( \delta_i \): boundary layer thickness.

\( D_i \): diffusion coefficient.

\( m \): mass of the substance produced at the electrode.

\( Q \): total electric charge passing through the plasma.

\( q \): electron charge.

\( v \): valence number of the substance as an ion (electrons per ion).
Modeling and Simulation of Chemical System Vaporization at High Temperature: Application to the Vitrification of Fly Ashes and Radioactive Wastes by Thermal Plasma

14. References

This book covers a number of topics in heat and mass transfer processes for a variety of industrial applications. The research papers provide advances in knowledge and design guidelines in terms of theory, mathematical modeling and experimental findings in multiple research areas relevant to many industrial processes and related equipment design. The design of equipment includes air heaters, cooling towers, chemical system vaporization, high temperature polymerization and hydrogen production by steam reforming. Nine chapters of the book will serve as an important reference for scientists and academics working in the research areas mentioned above, especially in the aspects of heat and mass transfer, analytical/numerical solutions and optimization of the processes.

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