1. Introduction

Coal is a combustible material applicable to a variety of oxidation scenarios with conditions ranging from atmospheric temperature to ignition temperature. One of the most frequent and serious causes of coal fires is self-heating or spontaneous combustion. Opening an underground coal seam to mine ventilation air, such as long-wall gob and goaf areas and coal stockpiles, creates a risk of spontaneous combustion or self-heating. Careful management and handling of coal stocks are required to prevent fires. Furthermore, the spontaneous combustion of coal also creates a problem for transportations on sea or land.

Generally, the self-heating of coal has been explained using the imbalance between the heat transfer rate from a boundary surface to the atmosphere and heat generation via oxidation reaction in the stock. The oxidation reaction depends on temperature and the concentrations of unreacted and reacted oxygen. When carbon monoxide exceeds a range of 100 to 200 ppm in the air around the coal and its temperature exceeds 50 to 55°C, the coal is in a pre-stage of spontaneous combustion. Thus, comprehensive studies of the mechanisms and processes of oxidation and temperature increase at low temperature (less than 50 to 55°C) have been investigated for long years.

Measurement of the heat generation rate using crushed coal samples versus constant temperature have been reported to evaluate its potential for spontaneous combustion. Miyakoshi et al. (1984) proposed an equation guiding heat generation in crushed coal via oxygen adsorption based on a micro calorimeter. Kaji et al. (1987) measured heat generation rate and oxygen consumption rate of three types of crushed coal at constant temperatures. They presented an equation to estimate heat generation rate against elapsed time. However, their time was defined under a constant temperature of coal, thus it is not able to be applied for the process with changing temperature of coal.

According to our observations of surface coal mines, the spontaneous combustion of coal initiates at coal seam surfaces as "hot spots," which have temperatures ranging from around 400 to 600 °C. Generally, the hot spot has a root located at a deeper zone from the outside surface of the coal seam or stock that is exposed to air. When the hot spot is observed on the surface, it is smoldering because of the low oxygen concentration. The heat generation rate from coal in the high temperature range (over 60°C) follows the Arrhenius equation, which is based on a chemical reaction rate that accelerates self-heating. Brooks and Glasser (1986) presented a simplified model of the spontaneous combustion of coal stock using the Arrhenius equation to estimate heat generation rate. They used a natural convection model...
to serve as a reactant transport mechanism. Carresl & Saghafil (1998) have presented a
numerical model to predict spoil pile self heating that is due mainly to the interaction of coal
and carbonaceous spoil materials with oxygen and water. The effects of the moisture content
in the coal on the heat generation rate and temperature are not considered in this chapter.
However, Sasaki et al. (1992) presented some physical modeling of these effects on coal
temperature.
Yuan and Smith (2007) presented CFD modeling of spontaneous heating in long-wall gob
areas and reported that the heat has a corresponding critical velocity. However, when the
Arrhenius equation is used for a small coal lump, the calculation does not show a return to
atmospheric temperatures. This can be seen from the data shown in Fig. 1. The reason, that
the results cannot be applied to small amounts of coal stock, may be a type of ageing effect.
Nordon (1979) proposed this as a possible explanation using the Elovich equation that has
been used in adsorption kinetics based on the adsorption capacity. He also presented a
model for the self-heating reaction of coal and identified two steady-state temperature
conditions one less than and one over 17°C. He also commented that the transport processes
of diffusion and convection take the mobile reactant, oxygen, from the boundary to the
distributed reaction where heat energy is released, and then convey the latter back to the
boundary. However, his concept is difficult to apply to numerical models.
In this chapter, a model is presented for spontaneous combustions of coal seam and coal
stock. It is based on time difference between thermal diffusion and oxygen diffusion.
Furthermore, the concept of “Equivalent Oxidation Exposure Time (EOE time)” is
presented. Also, we compared the aging time to the oxidation quantity to verify the
mechanism presented. Numerical simulations matching both the thermal behaviors of large
stocks and small lumps of coal were performed.

2. Mechanism of temperature rise in a large amount of coal stock
Coal exposed to air is oxidized via adsorbed oxygen in temperature ranges. It has a different
time dependence than that expressed by the Arrhenius equation, which guides this behavior
in the high temperature range. The adsorption rate of oxygen decreases with increasing time
for a constant temperature, because coal has a limit of oxygen consumption.
A schematic showing the process of spontaneous combustion is shown in Fig. 2. Assume a
coil stock has all but its bottom surface exposed to air of oxygen concentration, \( C_0 \) and and
temperature, $\theta_0$. Oxidation heat is generated in the coal is started from outside surface of the stock, because oxygen is supplied from the atmosphere. Some heat is lost to the atmosphere, but some also diffuse to inward to the center of the stock. The outer part of the stock returns to the atmospheric temperature, $\theta_0$, after enough time. However, the oxygen concentration of the inside stock is kept at a relatively low concentration, because oxygen does diffuse to the inner zone via the oxidation zone. When coal at the center of the stock is preheated slowly without oxygen, a high temperature spot at the center is generated.

The oxidation and heat generation zone gradually moves from the stock surface to the center while shrinking and rising in temperature. Finally a hot spot is formed at the center (see Fig. 2 (a) to (c)). Oxygen diffuses to center region after formation of the hot spot. This time delay of oxygen diffusion allows the coal temperature to rise exponentially in the center by long preheating and inducing smaller EOE time (see 3.3). Thus, the greater the volume in the coal stock, the more delay between preheating and oxygen diffusion.

After formation of the hot spot in the center, the coal begins to burn slowly without flames and projects toward the outer surface through paths with relatively high effective diffusivity, which has greater oxygen concentration than the surrounding coal. Finally, the hot spot appears on the outside surface of the stock, which marks the start of spontaneous.

Fig. 2. Schematic process showing spontaneous combustion of large amount of coal stock, (a), (b) and (c): Hot spot forming process with accumulating heat and shrinking zone of oxidation and preheating zone, (d): Projection growth of hot spot toward to stock surface through high permeable path
3. EOE time and heat generation rate of coal

3.1 Heat generation rate from coal

In the present model, coal oxidation reaction includes physical adsorption and chemical adsorption via oxygen reaction at low temperatures. Measurements of the heat generation rate at the early stages of the process that show an exponential decrease have been reported by many experiments, such as Kaji et al. (1987), shown in Fig. 3, and Miyakoshi et al. (1984). Based on their measurement results, the heat generation rate per unit mass of coal at temperature \( \theta \) (°C), \( q \) (W/g or kW/kg), can be expressed with a function of elapsed time after being first exposed to air, \( \tau \) (s):

\[
q = C \cdot A \exp(-\gamma \tau)
\]  
(1)

where, \( A \) (kW/kg) is heat generating constant, \( C \) is molar fraction of oxygen, and \( \gamma \) (s\(^{-1}\)) is the decay power constant. The initial order of heat generating rate of coal for exposing air is \( q(0) \approx 0.01 \) to 0.001 kW/kg.

![Graph showing heat generation rate vs. exposure time for constant temperatures](https://example.com/figure3.png)

Fig. 3. Models of heat generating rate of coal vs. exposure time for constant temperatures

3.2 Arrhenius equation for coal oxidation

Kaji et al. (1987) measured rates of oxygen consumption due to coal oxidation in the temperature range 20 to 170 °C using coals ranging from sub-bituminous to anthracite coal. They reported that heat generated per unit mole of oxygen at steady state is \( h = 314 \) to 377 (kJ/mole), and their results of the Arrhenius plots, the oxygen consumption rate versus inverse of absolute temperature \( T^{-1} \) (K\(^{-1}\)), shows the Arrhenius equation. Thus, the higher the coal temperature; the faster the oxidation or adsorption rate is given. When the heat generation rate is proportional to oxygen consumption rate, the heat generated, \( A \), can be estimated using the following equation,

\[
A = A_0 \cdot \exp\left(-\frac{E}{RT}\right)
\]  
(2)
where, \( A_0 \) (kW/kg) is pre-exponential factor for \( A \), \( E \) (J/mole) is the activation energy, \( R \) is gas constant (J/mol/K), and \( T = (273+\theta) \) (K) is absolute temperature. Kaji et al. (1987) has reported that the coals have almost the same activation energy of around \( E \approx 50 \) kJ/mole for temperature range of 20 to 170 °C. On the other hand, Miyakoshi et al. (1984) reported as \( E \approx 20 \) kJ/mole for Japanese coals in temperature range lower than 50 °C based on measurements of oxygen adsorption heat using with a micro-calorimeter. The activation energy of fresh coal is expected as much lower than that of exposed coal in the air, because fresh coal adsorbs oxygen physically at an initial stage of self-heating. Average activation energy and decay power constant, presented by Miyakoshi et al. for Japanese bituminous coals (see Tables 1 and 2), were used for present numerical simulations.

3.3 Equivalent oxidation exposure time

The heat generating rate, \( q \), is expressed as a function of \( \theta \), \( C \), and \( t \). Equations (1) and (2) can be used to calculate \( q \) for a constant temperature. However, they are not applicable for the calculation of the normal coal temperature change versus elapsed time. Its concept is partly similar to Elovich equation, but it provide a scheme to estimate \( q \) follows change of temperature of coal and EOE time.

For an example, assume a coal lump is placed in an environment in which \( C = 0.1 \) and \( \theta = 45°C \), for elapsed time; \( t = 1 \) h, and then is stored in other one of \( C = 0.2 \) and \( \theta = 70°C \) for another 1 h period. It is not possible to reconstruct this situation by adding the former and later times with different oxidation rates. A new model of the elapsed time that considers the aging degree of the coal is required to overcome this difficulty. The cumulative generated heat of the coal, \( Q_m \) (J/g) from elapsed time 0 to \( t \), is defined as,

\[
Q_m' = \int_0^t q'(\theta', C', t') dt'
\]

where, the actual heat generation rate, \( q'(\theta', C', t') \), \( \theta' \) and \( C' \) are changing with the elapsed time, \( t' \). However, the cumulative heat, \( Q_m \), for constant \( \theta \) and \( C \), can be derived using Equations (1) and (2) from time 0 to \( \tau^* \):

\[
Q_m = \int_0^{\tau^*} q(\theta, C, t') dt' = \frac{CA}{\gamma} \left( 1 - \exp(-\gamma \tau^*) \right) = Q_m
\]

If the amounts of accumulated heat, \( Q_m' \) and \( Q_m \), defined in Equations (3) and (4), are equal, \( \tau^* \) in Eq. (4) expresses the aging time of the coal for constant temperature; \( \theta = \theta'(t) \) and constant concentration; \( C=C'(t) \), for the actual elapsed time \( (t'=t) \). In this paper, \( \tau^* \) is defined as the EOE time (see Fig. 4). It is calculated based on a summation of generated heat \( q'(\theta', C', t') \Delta t' \) over a numerical calculation interval time, \( \Delta t' \). It is expressed by the following single-calculation equation:

\[
\tau^* = \frac{1}{\gamma} \ln \left[ 1 - \frac{\gamma}{CA} \left( \sum_i q'_i \Delta t'_i \right) \right]
\]
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\[ Q_m = \int_0^{t'} q'(\theta', C', t')dt' \]

Heat Generating Rate, \( q'(\theta', C', t') \) (actual)

\[ Q_m = \int_0^{t^*} q(\theta, C, t')dt' \]

\( t, C \)

\( q(\theta', C', t') \)

Fig. 4. Schematic definition of EOE-time of coal to estimate heat generating rate by matching total heat generations

The most important characteristic of the EOE is that if a part of coal releasing heat to its surrounding, its EOE time is increased. It means that receiving heat makes smaller EOE time due to temperature increasing. Using the EOE time, the actual heat generating rate of coal at \( t \) can be obtained by substituting \( t^* \) instead of \( t \) into Eq. (1).

\[ q'(t) = C(t) \cdot A_0 \cdot \exp \left( -\frac{E / R}{273 + \theta(t)} \right) \exp(-\gamma t^*) \]  

(6)

Assuming the reaction heat of unit volume of oxygen is \( \Delta H \), the oxygen consumption rate, \( v' \), and the accumulated consuming oxygen, \( V' \), are given by:

\[ v'(t) = \frac{q}{\Delta H} \]  

(7)

\[ V'(t) = \int_0^{t^*} v'(\theta', C', t')dt' \]  

(8)

The reaction heat of unit volume of oxygen was evaluated as \( \Delta H \approx 16 \) (J/cm\(^3\)O\(_2\)) based on the experimental results of heat generation rate by Kaji et al.(1987) and Miyakoshi et al.(1984) shown in Fig. 3. The oxygen consumption rate is used in the oxygen diffusion equation for its concentration.

3.4 Thermal conduction and diffusivity of coal stock consisting porous media

For a case of coal stock, thermal characteristics are required for a porous media consisting lump coals and air. Thermal conductivity of a porous media is dependent on the porosity or void fraction, \( \varepsilon \), and specific internal surface area in it. Kunii & Smith (1960) have presented the equations predicting an effect of porosity and thermal conductivities of solid and fluid on the heat transfer properties. They have presented effective thermal conductivity of porous media versus porosity, \( \varepsilon \). In present model of a coal stock, effective thermal conductivity can be estimated by a following equation revised from the Kunii & Smith’s equation by omitting term of the thermal radiation effects due to low temperature range,
Fig. 5. Effective thermal conductivity vs. porosity of coal stock in the air evaluated by Kunii & Smith’s equation (1960) (a case for $\lambda_{coal}/\lambda_{air} = 13.3$)

$$\frac{\lambda}{\lambda_{coal}} = \varepsilon \frac{\lambda_{air}}{\lambda_{coal}} + \frac{1 - \varepsilon}{\Phi \frac{\lambda_{coal}}{\lambda_{air}} + \frac{2}{3}}$$

(9)

where $\lambda$ is effective thermal conductivity of coal stock, $\lambda_{coal}$ is thermal conductivity of lump coal, $\lambda_{air}$ is thermal conductivity of air, and $\Phi$ is a ratio of effective thickness of air film over coal lump diameter given against $\varepsilon$ that is classified into three regime of $\varepsilon \geq 0.476$ (loose packing/unconsolidated), $0.476 > \varepsilon \geq 0.260$ and $\varepsilon < 0.260$ (close packing/consolidated) adapted by Kunii & Smith (1960). Volumetric heat capacity, $\rho C_p$ (J/kg), and thermal diffusivity of the coal stock, $\alpha$ (m$^2$/s) are derived from following equations,

$$\rho C_p = \varepsilon \rho_{air} C_{p air} + (1 - \varepsilon) \rho_{coal} C_{p coal}$$

(10)

$$\alpha = \frac{\lambda}{\rho C_p}$$

(11)

Suppose $\lambda_{coal}/\lambda_{air} = 13.3$ or, $\lambda_{coal} = 0.36$ W/m/$^\circ$C for a typical thermal conductivity of coal, the effective thermal conductivity, $\lambda$, calculated by Eq. (9) is shown in Fig. 5 with thermal conductivity of linear parallel model; $\lambda = \lambda_{coal}(1 - \epsilon) + \epsilon \lambda_{air}$. The effective thermal conductivity is lower than that of the linear parallel model, because air in coal stock gives a thermal resistance around coal lumps because of low thermal conductivity of air.

<table>
<thead>
<tr>
<th>Coal Density</th>
<th>Specific Heat of Coal</th>
<th>Thermal diffusivity of Coal</th>
<th>Diffusion Coefficient</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\rho_{coal}$</td>
<td>$C_p$</td>
<td>$\alpha$</td>
<td>$D$</td>
</tr>
<tr>
<td>1291 kg/m$^3$</td>
<td>1210 J/kg/$^\circ$C</td>
<td>6.8x10$^{-8}$ m$^2$/s</td>
<td>7.1x10$^{-6}$ m$^2$/s</td>
</tr>
</tbody>
</table>

Table 1. Thermal properties of coal for present numerical simulations
Heat Analysis and Thermodynamic Effects

<table>
<thead>
<tr>
<th>Decay power constant</th>
<th>Pre-exponential factor</th>
<th>Activation energy</th>
</tr>
</thead>
<tbody>
<tr>
<td>$3.0 \times 10^{-4}$ s$^{-1}$</td>
<td>$2.9 \times 10^{4}$ W/kg/kg</td>
<td>$2.0 \times 10^{4}$ J/mol</td>
</tr>
</tbody>
</table>

Table 2. Heat generating properties of coal for present numerical simulations

![Diagram of heat generating properties](image)

Fig. 6. Model definition of a sphere lump coal exposed to atmospheric air

4. Numerical simulation results and discussion

In this section, numerical simulations for three kinds of coal stock model carried out by authors are introduced to show the effectiveness of the EOE time simulating self-heating process of the coal stocks. Those were done using the finite difference method to solve the equations on heat transfer and oxygen advection and diffusion. Number of blocks used in the simulation was 100 for one-dimensional model and 10000 for two-dimensional model. Time interval of the numerical simulations was adapted as 20s to satisfy enough accuracy.

4.1 Sphere lump coal exposed to atmospheric air

The simulations on coal lump were carried out for simple one-dimensional sphere model as shown in Fig. 6. Its outer surface is open to air with constant temperature and constant O$_2$ concentration. Thus, oxygen is provided by molecular diffusion expressed as:

$$\frac{\partial \theta}{\partial t} = \alpha \left( \frac{2 \partial^2 \theta}{r \partial r^2} + \frac{\partial^2 \theta}{\partial r^2} \right) + \frac{q}{C_p}$$  \hspace{1cm} (12)

$$\varepsilon \frac{\partial C}{\partial t} = D \left( \frac{2 \partial C}{r \partial r} + \frac{\partial^2 C}{\partial r^2} \right) - \rho v_a$$  \hspace{1cm} (13)

$$\begin{align*}
\theta & = \theta_0 \\
C & = C_0
\end{align*}$$  \hspace{1cm} (14)

The thermal and heat generating properties of the coal seam used in the simulations are listed in Tables 1 and 2. Gas permeability, $K$, and diffusion coefficient, $D$, of lump coal and
close packing of crushed coal were measured, and the correlated equations have been presented by Sasaki et al. (1987). The boundary conditions of temperature and oxygen concentration at the outer surface were fixed with constants expressed by Eq.(14).

![Fig. 7. Temperature at sphere center vs. elapsed time for different diameter](image1)

![Fig. 8. Oxygen concentration at sphere center vs. elapsed time for different diameter](image2)
Fig. 9. Ratio of EOE time over elapsed time at sphere center of coal lump vs. elapsed time for different diameter

Figures 7 to 9 show the numerical simulation results on temperature, oxygen concentration and ratio of EOE time over elapsed time at the sphere center versus elapsed time for different diameter $d_0 = 0.3$ to 10m. The temperature at center of the stock is increased with elapsed time, but the cases of $d_0 \leq 2$ m show the temperature return to atmospheric and initial temperature $\theta_0 = 25 ^\circ$C. This is because that the EOE time increased by heat transfer to surrounding air makes reducing heat generation rate of coal lump even if its location is at the center. However, the case of $d_0 \geq 4$ m, coal at the sphere center receiving enough heat in low oxygen concentration before oxygen diffuses into the center, and lower EOE time induces higher heat generation than that of $d_0 \leq 2$m before ignition and combustion of coal. The critical diameter is evaluated roughly as $d_0 = 3$m for present model, it depends on the activation energy, $E$ and the decay power constant, $\gamma$, of the coal.

4.2 A model of coal seam remained at goaf area in underground mines

In Fig. 10, a simple one-dimensional numerical model for a coal seam remained at goaf area that is cavity area behind a longwall working in underground coal mines. It is expected to expose to relatively high temperature air of 45 °C. Its faces are open to air with ventilation pressure difference in the goaf area, $\Delta p = 10$ mmH$_2$O= 98Pa. Thus, oxygen is provided by not only molecular diffusion, but also permeable airflow between two faces. Therefore, oxygen in the air diffuses from both ends and adsorbs in micro pores of the coal seam as it diffuses toward the center of the seam.

The thermal and heat generating properties of the coal seam used in the simulations are listed in Tables 1 and 2. In this study, the effects of the moisture content in the coal on the heat generation rate and temperature are not considered. However, Sasaki et al. (1992) presented some physical modeling of these effects on coal temperature.
The coal seam is \( L = 5.0 \) m in length, has effective diffusion coefficient of \( D = 7.1 \times 10^{-6} \) m\(^2\)/s, and permeability of \( K_0 = 10 \) to 100 md \( \approx 10^{-15} \) to \( 10^{-14} \) m\(^2\).

The results showing the temperature distribution are shown in Fig. 11. The zone with rising temperature and high oxygen consumption gradually moves toward the center and its maximum temperature also increases. The present results are similar to the simulation results presented by Nordon (1979), but temperature of the outer layer near the boundary surface decreases with the decreasing heat generation rate. This drop in the heat generation rate is due to increasing EOE time in the outer layer. As shown in Fig. 12, the larger the permeability, the larger the EOE time of the outer layer of the stock.

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Oxygen in the ventilation air diffuses from both faces of the coal seam toward its center region under the lowest oxygen concentration due to absorption at outer regions as shown in Fig. 13. It takes much longer time to make higher oxygen concentration in the center region.

![Fig. 11. Transition of temperature distribution of coal seam (L=5m, Initial temperature, \( \theta(0) = \theta(L) = 45^\circ C \), outer oxygen concentration, \( C(0) = C(L) = 0.20 \), permeability \( K_0 = 50 \text{ md} = 4.9 \times 10^{-14} \text{ m}^2 \), \( D = 7.1 \times 10^{-6} \text{ m}^2/\text{s} \)](image_url)

![Fig. 12. Simulation results of EOE-time for different permeability of coal seam (L=5m, \( \theta(0) = \theta(L) = 45^\circ C \), t = 180 days, outer oxygen concentration, \( C(0) = C(L) = 0.20 \))](image_url)
Nield & Bejan (1999) have presented numerical models and applications for convection flows in a porous media. Spontaneous combustion in a coal seam, that is consolidated porous media, has been modelled and analyzed by numerical simulations. The simulation was performed using the finite difference method to solve the equations of heat transfer, oxygen diffusion and permeable flow via ventilation pressure difference. The EOE time has been applied to numerical simulations on spontaneous self-heating of coal stocks. The numerical simulations of the coal stock were performed while accounting for the natural convection flow and heat transfer in the stock as a porous media with two dimensional simulation model, which shown in Fig. 14. The right-hand region of width \( W \) and height \( H \) (\( x = 0 \) to \( W \), \( z = 0 \) to \( H \)) was calculated using its symmetry about \( x = 0 \).

By solving equations of stream function, \( \psi \), and boundary condition at outer surface (\( x = L \) and \( z = H \)), the natural convection flow velocities (\( u, w \)) in horizontal(\( x \)) and vertical(\( z \)) directions (\( x, z \)) are expressed by numerical analysis with two dimensional equations for heat transfer and oxygen diffusion for the stock that is expanded from equations in one dimension described in former sections 4.1 and 4.2 (see Nield & Bejan, 1999). The numerical simulations were done using with 900 to 1800 blocks for the coal stock models.

Fig. 14. Two-dimensional coal stockyard model with internal natural convection flow
Fig. 15. Nusselt number, $N_u$ vs. Reynolds number, $Re=\nu\delta/\nu_{air}$ in porous media consisting lump coals and air

$$\frac{\partial^2 \Psi}{\partial x^2} + \frac{\partial^2 \Psi}{\partial z^2} = \frac{K}{\mu_{air}} \beta \frac{\partial \theta}{\partial x} \tag{19}$$

$$u = \frac{\partial \Psi}{\partial x}; \quad w = -\frac{\partial \Psi}{\partial z} \tag{20}$$

where $K$ is permeability of coal stock, $\beta$ is thermal expansion coefficient of air, $\mu_{air}$ is air viscosity and $g$ is acceleration of gravity. The boundary conditions at $x=0, W$ and $z=0, H$ are,

$$\Psi = 0 \text{ at } x = 0; \quad \frac{\partial \Psi}{\partial x} = 0 \text{ at } z = W \tag{21}$$

$$\Psi = 0 \text{ at } z = 0; \quad \frac{\partial \Psi}{\partial z} = 0 \text{ at } z = H$$

A model on heat transfer rate between lump coals or coal matrix and airflow is needed to simulate internal temperature distribution in the stock. Wakao & Kaguei(1982) reviewed the effective heat transfer coefficient, $a$, for unconsolidated porous media. Expressions of Nusselt number, $N_u(=a\delta/\lambda)$, have been presented by for the interstitial heat transfer coefficients in porous media as shown in Fig. 15. From the figure, $N_u$ is roughly proportional to square root of the Reynolds number, $R_e^{1/2}$, and it matches fairly well with equations presented by Kunii & Smith(1960), Kunii & Suzuki and Wakao & Kaguei(1982). In present numerical simulations, an approximated equation on heat transfer per unit volume, $\Delta q$ ;

$$\Delta q = a(\theta_{air} - \theta)\xi = 1.6R_e^{1/2} \frac{(\theta_{air} - \theta)\xi}{\delta} \lambda_{air} \tag{22}$$

where $\theta_{air}$ is air flow temperature, $\theta$ is lump coal temperature and $\xi$ is internal surface area in the unit volume of the coal stock. $\Delta q$ is used to calculate natural convection air flow temperature $\theta_{air}$ and lump coal temperature $\theta$ with heat generation rate of coal lump as $q+\Delta q$. 

The coal stock $W$ in width and $H$ in height was simulated with the stock conditions; $C_0=0.2$, $\theta_0=30^\circ{}C$, $K=1.1\times10^5$ d and $D=3.4\times10^{-4}$ m$^2$/s. The stock bottom at $z=0$ is set as adiabatic and impermeable boundary. Natural convection airflow in the stock is observed in Fig. 16 as that flow comes from side walls toward the center of the stock. It controls temperature rise, cooling, and oxygen supply. High temperature region that was generated at center and upper in the stock after $t=100$ h. But the natural convection flow and distribution of oxygen concentration are complicated with rapid changing in early stage; $t=0$ to 100 h of self-heating of coal stock (see Fig. 17). The region is also downstream of the convective airflow with low oxygen concentration but high temperature. The convection flow becomes faster with rising internal temperature. The mechanisms controlling the temperature rise are complex and affected by the EOE time. The temperature and convective flow velocity are affected each other, and coal temperature determines not only the heat generation rate by supplying oxygen, but also the cooling or heating rate proportional to temperature difference between air and coal lumps.

A comparison of simulation results for different aspect ratios; $W/H = 1$ and $2$ is shown in Fig. 18. It is interesting that center region of longer ratio $W/H= 2$ shows relatively lower temperature compared with outer region. The reason is the internal natural convection flow from side walls is coming up to upper surface before closing to center region. Thus, the temperature distribution of right region is similar even if the aspect ratio is different.

Figure 19 shows the maximum temperature in the stock, $\theta_{\max}$, versus the elapsed time, $t$, for different aspect ratios $W/H = 1$ and $2$. It rises to a temperature between 47 and 52$^\circ{}C$ in less than $t=100$ h, then holds this temperature during $t=30$ to 300 hours. Finally, the temperature decreases with time, because of the increasing the EOE time by releasing heat to the atmosphere. The natural convection airflow provides oxygen, but suppresses the maximum temperature in the stock by cooling effect and makes heat transfer increasing with the temperature difference to air temperature in atmosphere.

![Fig. 16. Streamlines of internal natural convection flow and temperature distribution at $t = 500h$ in coal stock ($2W=10m$, $H=5m$, $C_0=0.2$, $\theta_0=30^\circ{}C$, $K=1.1\times10^5$ d, $D=3.4\times10^{-4}$ m$^2$/s)](image)

Finally the simulation was done to get matching with a monitored temperature at a coal stockyard carried out by Coal Mining Research Center, Japan (CMRCJ, 1983). As shown in Fig. 20, a model of a coal stockyard is 30m in width and 5m in height with trapezoid shape. On the other hand, the simulation model is just rectangle shape consists same thermal and flow characteristics of the coal stock defined in Fig. 14. The temperature at the point in coal...
stockyard was compared. It shows fairly well matching with the monitored temperature data to corresponding position.

![Image of oxygen concentration distribution](image1)

**Fig. 17.** Change of oxygen concentration distribution of two-dimensional coal stock (right half, $2W=10m$, $H=5m$, $K=1.1\times10^8$ d, $D=3.4\times10^4$ m$^2$/s) with internal natural convection flow.

![Image of temperature distribution](image2)

**Fig. 18.** Effect of aspect ratio, $H/W$, on temperature distribution in two-dimensional coal stock with internal natural convection flow ($2W=10m$, $H=5m$, $K=1.1\times10^8$ d, $D=3.4\times10^4$ m$^2$/s).

An important result of the numerical simulations is that the oxidation of coal in the low temperature range reduces heat generating rate, because it provides cooling air accelerates increasing the EOE time. This could be used to ensure that coal stocks are kept within a safety level that prevents spontaneous combustion. Turnover of coal stocks at regular intervals works by increasing EOE time and releasing heat from center region of the stock.

![Image of maximum temperature transition](image3)

**Fig. 19.** Numerical simulation results of the maximum temperature transition in coal stock with three different aspect ratios.
5. Summary

In this chapter, a thermal mechanism of spontaneous combustion of coal seams and stocks in low temperature has been described. It has been discussed that the reason to enhance self-heating of coal stocks is the time delay between preheating from thermal diffusion and oxygen provided via diffusion. Especially, preheating without supplying oxygen makes a situation with high risk of spontaneous combustion. Another important mechanism discussed is the formation of a hot spot through the shrinking of the heated oxidation zone from the outer layer toward into the center region of the coal stock.

Heat generating of coal via the oxidation at low temperature includes complex functions of temperature and elapsed time. Thus, numerical models using only the Arrhenius equation to express heat generating of coal bases on its temperature are not able to simulate actual heat and mass transfer phenomena.

The concept of equivalent oxidation exposure time (EOE time) has been introduced to express time decay of coal oxidation. We have used this concept to simulate the heat generation while considering coal aging; that is, the ratio of the cumulative amount of oxidation to its oxidation capacity. This concept allowed us to consider these factors using simple calculation procedures following temperature changing of the coal. The physical model agrees with some experimental measurements with decay rate of heat generating from coal during exposure to oxygen. It has been successfully applied to simulate the temperature of rump coal, coal seam and coal stock, which are exposed to ventilated or atmospheric air. We used the finite difference method to solve the equations of thermal diffusion, heat transfer, and oxygen diffusion in these models. For the case of the coal stock, natural convection flow was also considered. The results showed that natural convection flow provides oxygen, but suppresses the maximum temperature of the stock by convective heat flow moving to the atmosphere.

Low temperature oxidation of coal with cooling accelerates the increase of the EOE time and reduces heat generation rate to an inherently safe level. Turnovers of lump coals in the stock at regular intervals are expected to prevent spontaneous combustion effectively by increasing the EOE time; not only by releasing heat in the center of the stock.
6. Acknowledgment

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7. Nomenclature

\[\begin{align*}
\alpha &= \text{effective heat transfer coefficient} \ [W/m^2/°C] \\
A &= \text{heat generating constant} \ [kW/kg] \text{ or } [W/g] \\
A_0 &= \text{pre-exponential factor for } A \ [kW/kg] \text{ or } [W/g] \\
C &= \text{oxygen concentration or molar fraction} \ [-] \\
C_0 &= \text{oxygen concentration in atmosphere} \ [-] \\
C_{P} &= \text{average specific heat of coal stock} \ [J/kg/°C] \\
C_{P_{air}} &= \text{specific heat of air} \ [J/kg/°C] \\
C_{P_{coal}} &= \text{specific heat of lump coal/coal seam} \ [J/kg/°C] \\
d_0 &= \text{outer diameter of coal lump/stock} \ [m] \\
D &= \text{effective diffusion coefficient} \ [m^2/s] \\
E &= \text{activation energy} \ [J/mole] \\
g &= \text{acceleration of gravity} \ [m/s^2] \\
H &= \text{height of two-dimensional coal stock} \ [m] \\
h_c &= \text{height of coal seam} \ [m] \\
h_r &= \text{height of upper and lower rock sediment layers} \ [m] \\
K &= \text{permeability of coal stock} \ [d] \text{ or } [m^2] \ (1 \ d=9.8\times10^{-13}m^2/s) \\
K_0 &= \text{permeability of coal seam} \ [md] \text{ or } [m^2] \ (1md=9.8\times10^{-16}m^2/s) \\
L &= \text{width of coal seam} \ [m] \\
N_u &= \text{Nusselt number} \ [-] \\
q &= \text{heat generation rate of coal} \ [W/g] \text{ or } [kW/kg] \\
Q_m &= \text{cumulative generated heat of coal} \ [J/g] \text{ or } [kJ/kg] \\
Q_m' &= \text{cumulative generated heat of coal} \ [J/g] \text{ or } [kJ/kg] \\
R &= \text{gas constant} \ [J/K/mol] \\
Re &= \text{Reynolds number} \ [-] \\
r &= \text{radius from center in coal lump/stock} \ [m] \\
r_o &= \text{outer radius of coal lump/stock} \ [m] \\
t &= \text{elapsed time} \ [s] \\
T &= \text{absolute temperature of coal} \ [K] \\
U &= \text{permeable flow velocity in a coal seam due to pressure difference} \ [m/s] \\
u &= \text{natural convection flow velocity in } x \text{ direction} \ [m/s] \\
V' &= \text{accumulated consuming volume of oxygen} \ [cm^3O_2/g] \text{ or } [m^3O_2/s \cdot kg] \\
v' &= \text{oxygen volume consumption rate} \ [cm^3O_2/s \cdot g] \text{ or } [m^3O_2/s \cdot kg] \\
W &= \text{half width of two-dimensional coal stock} \ [m] \\
w &= \text{natural convection flow velocity in } z \text{ direction} \ [m/s] \\
x &= \text{horizontal axis} \ [m] \\
z &= \text{vertical axis} \ [m] \\
a &= \text{effective thermal diffusivity of coal seam or coal stock} \ [m^2/s] \\
\beta &= \text{thermal expansion coefficient of air} \ [-] \\
\gamma &= \text{decay power constant} \ [1/s]
\end{align*}\]
ΔH = reaction heat of unit volume of oxygen [J/cm³O₂]

Δq = heat transfer per unit volume of coal stock [kW/m³] or [W/cm³]

δ = average diameter of lump coals in coal stock [m]

ε = porosity or void fraction [-]

Φ = ratio of effective thickness over coal lump diameter [-]

κ = coefficient of heat transmission from coal seam [m²/s]

λ = effective thermal conductivity of porous media [W/(m°C)]

λ_air = thermal conductivity of air [W/(m°C)]

λ_coal = thermal conductivity of lump coal [W/(m°C)]

λ_r = thermal conductivity of rock [W/(m°C)]

μ = air viscosity [Pas]

ξ = internal surface area in unit volume of coal stock [m³/m³] or [cm³/cm³]

τ = exposure time [s]

τ* = equivalent oxidation exposure (EOE) time [s]

ν_air = dynamic viscosity coefficient of air [m²/s]

ρ_air = air density [kg/m³]

ρ_coal = density of lump coal or coal seam [kg/m³]

θ = temperature of coal lump or coal stock [°C]

θ₀ = air or atmospheric temperature and initial coal temperature [°C]

θ_air = temperature of internal natural convection air flow in coal stock [°C]

ψ = stream function of two dimensional natural convection flow [m²/s]

8. References


The heat transfer and analysis on heat pipe and exchanger, and thermal stress are significant issues in a design of wide range of industrial processes and devices. This book includes 17 advanced and revised contributions, and it covers mainly (1) thermodynamic effects and thermal stress, (2) heat pipe and exchanger, (3) gas flow and oxidation, and (4) heat analysis. The first section introduces spontaneous heat flow, thermodynamic effect of groundwater, stress on vertical cylindrical vessel, transient temperature fields, principles of thermoelectric conversion, and transformer performances. The second section covers thermosyphon heat pipe, shell and tube heat exchangers, heat transfer in bundles of transversely-finned tubes, fired heaters for petroleum refineries, and heat exchangers of irreversible power cycles. The third section includes gas flow over a cylinder, gas-solid flow applications, oxidation exposure, effects of buoyancy, and application of energy and thermal performance index on energy efficiency. The forth section presents integral transform and green function methods, micro capillary pumped loop, influence of polyisobutylene additions, synthesis of novel materials, and materials for electromagnetic launchers. The advanced ideas and information described here will be fruitful for the readers to find a sustainable solution in an industrialized society.

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