1. Introduction

This chapter addresses the problem of controlling a three-phase Induction Motor (IM) without mechanical sensor (i.e. speed, position or torque measurements). The elimination of the mechanical sensor is an important advent in the field of low and medium IM servomechanism; such as belt conveyors, cranes, electric vehicles, pumps, fans, etc. The absence of this sensor (speed, position or torque) reduces cost and size, and increases reliability of the overall system. Furthermore, these sensors are often difficult to install in certain applications and are susceptible to electromagnetic interference. In fact, sensorless servomechanism may substitute a measure value by an estimated one without deteriorating the drive dynamic performance especially under uncertain load torque.

Many approaches for IM sensorless servomechanism have been proposed in the literature is related to vector-controlled methodologies. One of the proposed nonlinear control methodologies is based on Feedback Linearization Control (FLC), as first introduced by (Marino et al., 1990). FLC provides rotor speed regulation, rotor flux amplitude decoupling and torque compensation. Although the strategy presented by (Marino et al., 1990) was not a sensorless control strategy, fundamental principles of FLC follow servomechanism design of sensorless control strategies, such as (Gastaldini & Grundling, 2009; Marino et al., 2004; Montanari et al., 2007; 2006).

The purpose of this chapter is to present the development of two FLC control strategies in the presence of torque disturbance or load variation, especially under low rotor speed conditions. Both control strategies are easily implemented in fixed point DSP, such as TMS320F2812 used on real time experiments and can be easily reproduced in the industry. Furthermore, an analysis comparing the implementation and the limitation of both strategies is presented. In order to implement the control law, these algorithms made use of only two-phase IM stator currents measurement. The values of rotor speed and load torque states used in the control algorithm are estimated using a Model Reference Adaptive System (MRAS) (Peng & Fukao, 1994) and a Kalman filter (Cardoso & Gründling, 2009), respectively.

This chapter is organized as follows: Section 2 presents the fifth-order IM mathematical model. Section 3 introduces the feedback linearization modelling of IM control. A simplified
FLC control strategy is described in Section 4. The proposed methods for speed and torque estimation, MRAS and Kalman filter algorithms, respectively, are developed in Sections 5 and 6. State variable filter is used to obtain derivative signals necessary for implementation of the control algorithm, and this is presented in section 7. Digital implementation in fixed point DSP TMS320F2812 and real time experimental results are given in Section 8. Finally, Section 9 presents the conclusions.

2. Induction motor mathematical model

A three-phase N pole pair induction motor is expressed in an equivalent two-phase model in an arbitrary rotating reference frame (q-d), according to (Krause, 1986) and (Leonhard, 1996) according to the fifth-order model, as

$$\frac{d}{dt} I_{qs} = -a_{12} I_{qs} - \omega s I_{ds} + a_{13} a_{11} \lambda_{qr} - a_{13} N \omega \lambda_{dr} + a_{14} V_{qs} \tag{1}$$

$$\frac{d}{dt} I_{ds} = -a_{12} I_{ds} + \omega s I_{qs} + a_{13} a_{11} \lambda_{dr} + a_{13} N \omega \lambda_{qr} + a_{14} V_{ds} \tag{2}$$

$$\frac{d}{dt} \lambda_{qr} = -a_{11} \lambda_{qr} - (\omega s - N \omega) \lambda_{dr} + a_{11} L_m I_{qs} \tag{3}$$

$$\frac{d}{dt} \lambda_{dr} = -a_{11} \lambda_{dr} + (\omega s - N \omega) \lambda_{qr} + a_{11} L_m I_{ds} \tag{4}$$

$$\frac{d}{dt} \omega = \mu \cdot (\lambda_{dr} I_{qs} - \lambda_{qr} I_{ds}) - B \frac{J}{J} \omega - T_L \tag{5}$$

$$T_e = \mu \cdot J \cdot (\lambda_{dr} I_{qs} - \lambda_{qr} I_{ds}) \tag{6}$$

In equations (1)-(6): $I_s = (I_{qs}, I_{ds})$, $\lambda_s = (\lambda_{qr}, \lambda_{dr})$ and $V_s = (V_{qs}, V_{ds})$ denote stator current, rotor flux and stator voltage vectors, where subscripts d and q stand for vector components in (q-d) reference frame; $\omega$ is the rotor speed, the load torque $T_L$, electric torque $T_e$ and $\omega_s$ is the stationary speed, $\theta_0$ is the angular position of the (q-d) reference frame with respect to a fixed stator reference frame ($\alpha-\beta$), where physical variables are defined. Transformed variables related to three-phase (RST) system are given by

$$x_{\alpha\beta} = K \cdot x_{RST} \tag{7}$$

Let

$$x_{qd} = e^{j\theta_0} x_{\alpha\beta} \tag{8}$$

with $e^{j\theta_0} = \begin{bmatrix} \cos \theta_0 & -\sin \theta_0 \\ \sin \theta_0 & \cos \theta_0 \end{bmatrix}$ and $K = \sqrt{\frac{2}{3}} \begin{bmatrix} 1 & -\frac{1}{\sqrt{3}} & -\frac{1}{\sqrt{3}} \\ 0 & -\frac{\sqrt{3}}{2} & -\frac{\sqrt{3}}{2} \end{bmatrix}$.

$x_{qd}$ and $x_{\alpha\beta}$ stand for two-dimensional voltage flux and stator current vector, respectively on (q-d) and ($\alpha-\beta$) reference frame.

The relations between mechanical and electrical parameters in the above equations are

$$a_0 = L_s L_r - L_m^2, a_{11} = \frac{R_r}{L_r}, a_{12} = \frac{L_s L_r R_s}{a_0 L_s} + \frac{L_m^2}{a_0 a_{11}}, a_{13} = \frac{L_m}{a_0}, a_{14} = \frac{L_r}{a_0} \text{ and } \mu = \frac{N L_m}{J L_r}.$$
where $R_s$, $R_r$, $L_s$ and $L_r$ are the stator/rotor resistances and inductances, $L_m$ is the magnetizing inductance, $J$ is the rotor inertia, $B$ is the viscous coefficient and $N$ is the number of pole pairs. In the control design, the viscous coefficient of (5) is considered to be approximately zero, i.e. $B \approx 0$.

3. Feedback Linearization Control

The feedback Linearization Control (FLC) general specifications are two outputs - rotor speed and rotor flux modulus, as

$$y_1 = \begin{bmatrix} \omega \\ \sqrt{\lambda_{qr}^2 + \lambda_{dr}^2} \end{bmatrix}^T \Delta \equiv \begin{bmatrix} \omega \\ |\lambda_r| \end{bmatrix}^T \tag{9}$$

which is controlled by two-dimensional stator voltage vector $V_s$, on the basis of measured variables vector $y_2 = I_s$. The development concept of this control strategy is completely described in (Marino et al., 1990) and it will be omitted here. Following the concept of indirect field orientation developed by Blaschke, (Krause, 1986) and (Leonhard, 1996), the purpose of FLC control is to align rotor flux vector with the d-axis reference frame, i.e.

$$\lambda_{dr} = |\lambda_r| \quad \lambda_{qr} = 0 \quad \tag{10}$$

The condition expressed in (10) guarantees the exact decoupling of flux dynamics of (1)-(4) from the speed dynamics. Once rotor flux is not directly measured, only asymptotic field orientation is possible, according to (Marino et al., 1990) and (Peresada & Tonielli, 2000), then

$$\lim_{t \to \infty} \lambda_{dr} = |\lambda_r| \quad \lim_{t \to \infty} \lambda_{qr} = 0 \quad \tag{11}$$

It is defined $y_1^* = \begin{bmatrix} \omega_{ref} \\ \lambda_r^* \end{bmatrix}^T$, where $\omega_{ref}$ and $\lambda_r^*$ are reference trajectories of rotor speed and rotor flux. The speed tracking, flux regulation control problem under speed sensorless conditions is formulated considering IM model (1)-(5) under the following conditions:

(a) Stator currents are measurable;
(b) Motor parameters are known and considered constant;
(c) Load torque is estimated and it is applied after motor flux excitation;
(d) Initial conditions of IM state variables are known;
(e) $\lambda_r^*$ is the flux constant reference value and estimated speed $\hat{\omega}$ and reference speed $\omega_{ref}$ are the smooth reference bounded speed signals.

FLC equations are developed considering the fifth-order IM model under the assumption that estimated speed tracks real speed, and therefore it is acceptable to replace measured speed with estimated speed (i.e. $\hat{\omega}_k \approx \omega$). In addition, the torque value is estimated using a Kalman filter. Fig. 1 presents the block diagram of FLC Control.

3.1 Flux controller

From the decoupling properties of field oriented transformation (10), the control objective of the flux controller is to generate a flux vector aligned with the d-axis to guarantee induction motor magnetization.

Then, substituting (10) in (4)

$$i_{ds} = \left( a_{11} \lambda_r^* + \frac{d}{dt} |\lambda_r| \right) \frac{1}{a_{11} L_m} \quad \tag{12}$$
The rotor flux $|\lambda_r|$ is estimated by a model derived from the induction motor mathematical model, (3) and (4), that makes use of measured stator currents $(I_{qs}, I_{ds})$ and estimated speed $\hat{\omega}$ variables.

$$\frac{d}{dt} \lambda_r = -a_{11} \lambda_r - j(\omega_s - N\hat{\omega}) \lambda_r + a_{11} L_m I_s$$  \hspace{1cm} (13)$$

where the stationary speed is $\omega_s = N\hat{\omega} + \frac{a_{11} L_m}{\lambda_s} i_{qs}$. The digital implementation of the flux controller is made using Euler discretization and the derivative rotor flux signal is obtained by a state variable filter (SVF).

**3.2 Speed controller**

The speed control algorithm uses the same strategy adopted for the flux subsystem and it is computed from (5), as

$$i_q = \frac{1}{\mu \lambda_r^2} \left( \frac{\tau_L}{f} + \frac{d}{dt} \omega_{ref} \right)$$  \hspace{1cm} (14)$$

To compensate for speed error between estimated speed and reference speed, (i.e. $e_\omega = \hat{\omega} - \omega_{ref}$), a proportional integral compensation is proposed, as follows

Fig. 1. Feedback Linearization Control proposed
These gains values \((k_{p_{iq}}, k_{i_{iq}})\) are determined considering an induction motor mechanical model. The reference quadrature component stator speed current is derived from (14)-(15), as

\[
i_{qs}^* = i_q - \bar{i}_q
\]  

In DSP implementation, the speed controller is discretized using the Euler method and the rotor speed derivative (14) is computed by a SVF.

### 3.3 Currents controller

From (1) and (2), the currents controller is obtained, as

\[
u_{qs} = \frac{1}{a_{14}} \left( a_{12}i_{qs}^* + \omega s i_{ds}^* + a_{13}\lambda_r N (\omega_{ref} + e_\omega) + \frac{d}{dt} I_{qs} \right)
\]

and

\[
u_{ds} = \frac{1}{a_{14}} \left( a_{12}i_{ds}^* + \omega s i_{qs}^* + a_{11}a_{13}\lambda_r + \frac{d}{dt} I_{ds} \right)
\]

where proportional integral gains of the current error

\[
\tilde{u}_{qs} = \left( k_{pv} + \frac{k_{iv}}{s} \right) \tilde{i}_{qs}
\]

and

\[
\tilde{u}_{ds} = \left( k_{pv} + \frac{k_{iv}}{s} \right) \tilde{i}_{ds}
\]

in which \(\tilde{i}_{qs} = I_{qs} - i_{qs}^*\) and \(\tilde{i}_{ds} = I_{ds} - i_{ds}^*\).

These gains \((k_{pv}, k_{iv})\) are determined considering a simplified induction motor electrical model, which is obtained by load and locked rotor test. Hence, current controllers are expressed as

\[
\nu_{qs}^* = u_{qs} - \tilde{u}_{qs}
\]

and

\[
\nu_{ds}^* = u_{ds} - \tilde{u}_{ds}
\]

In DSP, currents controller are digitally implemented using discretized equation (17)-(22) based on the Euler method, and the stator current derivative is obtained by SVF using stator currents measures.

### 4. Simplified feedback linearization control

In order to reduce the number of computation requirements, a simplified feedback linearization control scheme is proposed. In this control scheme, one part of the current controller (6)-(7) is suppressed and only a proportional integral controller is used. This modification minimizes the influence of parameters variation in the control system.

Fig. 2 presents the block diagram of the Simplified FLC proposed.

The currents controller of simplified FLC are defined as
\[ v_{qs}^* = \left( k_{pv} + \frac{k_{iv}}{s} \right) \tilde{i}_{qs} \]  
(23)

\[ v_{ds}^* = \left( k_{pv} + \frac{k_{iv}}{s} \right) \tilde{i}_{ds} \]  
(24)

Fig. 2. Proposed Simplified Feedback Linearization Control

Flux and Speed Controller are computed exactly as in the previous scheme, as (12) and (14)-(16).

5. Speed estimation - MRAS algorithm

A squirrel-cage three-phase induction motor model expressed in a stationary frame can be modelled using complex stator and rotor voltage as in (Peng & Fukao, 1994)

\[ v_s = R_s i_s + L_s \frac{d}{dt} i_s + L_m \frac{d}{dt} i_r \]  
(25)

for squirrel-cage IM \( v_r = 0 \)

\[ 0 = R_r i_r - jN\omega L_r i_r - jN\omega L_m i_s + L_r \frac{d}{dt} i_r + L_m \frac{d}{dt} i_s \]  
(26)
The voltage and the current space vectors are given as $x = x_\alpha + jx_\beta$, $x \in \{v_\text{s}, i_\text{s}, i_\text{r}\}$, relative to the transformed variables present in (7). The induction motor magnetizing current is expressed by

$$i_\text{m} = \frac{L_r}{L_m}i_\text{r} + i_\text{s} \quad (27)$$

Two independent observers are derived to estimate the components of the counter-electromotive vectors.

$$\hat{e}_\text{m} = \frac{L^2_m}{L_r}i_\text{m} = \frac{L^2_m}{L_r} \left( \omega i_\text{m} - \frac{1}{T_r} i_\text{m} + \frac{1}{T_r} i_\text{s} \right) \quad (28)$$

$$e_\text{m} = v_\text{s} - R_s i_\text{s} - \sigma L_s \frac{d}{dt} i_\text{s} \quad (29)$$

where $\sigma = 1 - \frac{L_m}{L_s L_r}$. The instantaneous reactive power maintains the magnetizing current, and its value is defined by cross product of the counter-electromotive and stator current vector

$$q_\text{m} = i_\text{s} \otimes e_\text{m} \quad (30)$$

Substituting (28) and (29) for $e_\text{m}$ in (30) and noting that $i_\text{s} \otimes i_\text{s} = 0$, which gives

$$q_\text{m} = i_\text{s} \otimes \left( v_\text{s} - \sigma L_s \frac{d}{dt} i_\text{s} \right) \quad (31)$$

and

$$\hat{q}_\text{m} = \frac{L^2_m}{L_r} \left( (i_\text{m} \circ i_\text{s}) \omega + \frac{1}{T_r} (i_\text{m} \otimes i_\text{s}) \right) \quad (32)$$

Then, $q_\text{m}$ is the reference model of reactive power and $\hat{q}_\text{m}$ is the adjustable model. The estimated speed is produced by the proportional integral adaptation mechanism error of both models, and an MRAS system can be drawn as in Fig.3.

This algorithm is customary for speed estimation and simple to implement in fixed point DSP, such as in (Gastaldini & Grundling, 2009; Orlowska-Kowalska & Dybkowski, 2010; Vieira et al., 2009).

The SVF blocks are state variable filters and are explained in greater detail in Section 7. These filters compute derivative signals and are applied in voltage signals to avoid addition noise and phase delay among the vectors as was proposed by (Martins et al., 2006).

6. Load torque estimation - Kalman filter

The reduced mechanical IM system can be represented by the following equations

$$\frac{d}{dt} \begin{bmatrix} \omega \\ T_L \end{bmatrix} = \begin{bmatrix} -\frac{B_n}{J} & -\frac{1}{J} \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \omega \\ T_L \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} T_e \quad (33)$$

$$y = \begin{bmatrix} 1 & 0 \end{bmatrix} \begin{bmatrix} \omega \\ T_L \end{bmatrix} \quad (34)$$

The Kalman Filter could be used to provide the value of torque load or disturbances - $T_L$. Since (15)-(16) is nonlinear, the Kalman filter linearizes the model at the actual operating
Fig. 3. Reactive Power MRAS Speed Estimation

point (Aström & Wittenmark, 1997). In addition, this filter takes into account the signal noise, which could be generated as pulse width modulation drivers. Assuming the definitions

\[ x_k = \begin{bmatrix} \hat{\omega}_k & \hat{T}_L \end{bmatrix}^T, \quad A_m = \begin{bmatrix} -\frac{B_n}{T} & -\frac{1}{T} \\ 0 & 0 \end{bmatrix}, \quad B_m = \begin{bmatrix} 1 \\ 0 \end{bmatrix}, \quad C_m = \begin{bmatrix} 1 & 0 \end{bmatrix} \text{ and } y_k = \hat{\omega}. \]

Then, the recursive equation for the discrete time Kalman Filter (De Campos et al., 2000) is described by

\[ K(k) = P(k)C_m^T \left( C_mP(k)C_m^T + R \right)^{-1} \] (35)

where \( K(k) \) is the Kalman gain. The covariance matrix \( P(k) \) is given by

\[ P(k+1) = (I - A_m t_s) \left( P(k) - K(k)C_mP(k) \right) (I - A_m t_s)^T + (B_m t_s) Q (B_m t_s)^T \] (36)

Therefore, the estimated torque \( \hat{T}_L \) is one observed state of the Kalman filter

\[ \hat{x}_k(k+1) = (I - A_m t_s) \hat{x}_k(k) + B_m t_s u(k) + (I - A_m t_s) K(k) \left( \hat{\omega} - C_m \hat{x}_k(k) \right) \] (37)

giving \( \hat{\omega} \approx \hat{\omega}_k \) and \( \hat{x}_k(k) = \begin{bmatrix} \hat{\omega}_k & T_L \end{bmatrix}^T. \)

The matrices \( R \) and \( Q \) are defined according to noise elements of predicted state variables, taking into account the measurement noise covariance \( R \) and the plant noise covariance \( Q \).

7. State variable filter

The state variable filter (SVF) is used to mathematically evaluate differentiation signals. This filter is necessary in the implementation of PLC and MRAS algorithms. The transfer function of SVF is of second order as it is necessary to obtain the first order derivative.

\[ G_{svf} = \frac{\omega_{svf}}{(s + \omega_{svf})^2} \] (38)
where $\omega_{svf}$ is the filter bandwidth defined at around 5 to 10 times the input frequency signal $u_{svf}$.

The discretized transfer function, using the Euler method, can be performed in state-space as

$$x_{svf}(k + 1) = A_{svf}x_{svf}(k) + B_{svf}u_{svf}(k)$$

(39)

where $A_{svf} = \begin{bmatrix} 1 & 0 \\ -\omega_{svf}^2 & 1 - 2\omega_{svf} \end{bmatrix}$, $B_{svf} = \begin{bmatrix} 0 \\ \omega_{svf}^2 \end{bmatrix}$ and $x_{svf} = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$.

The state variables $x_1$ and $x_2$ represent the input filtered signal and input derivative signal.

**8. Experimental results**

Sensorless control schemes were implemented in DSP based platform using TMS 320F2812. Experimental results were carried out on a motor with specifications: 1.5cv, 380V, 2.56A, 60 Hz, $R_s = 3.24\Omega$, $R_r = 4.96\Omega$, $L_r = 404.8mH$, $L_s = 402.4mH$, $L_m = 388.5mH$, $N = 2$ and nominal speed of 188 rad/s.

The experimental analyses are carried out with the following operational sequence:

1) The motor is excited (during 10 s to 12 s) using a smooth flux reference trajectory.
2) Starting from zero initial value, the rotor speed reference grows linearly until it reaches the reference value. Thus, the reference rotor speed value is kept constant.
3) During stand-state, a step constant load torque is applied.

In order to generate load variation for torque disturbance analyses, the DC motor is connected to an induction motor driving-shaft. Then, the load shaft varies in accordance with DC motor field voltage and inserting a resistance on its armature. Fig. 4 and Fig. 5 depict performance of both control schemes: FLC control and simplified FLC control with rotor speed reference of 18 rad/s. In these figures measure speed, estimated speed, stator (q-d) currents and estimated torque are illustrated.

Fig.6 and Fig. 7 present experimental results with 36 rad/s rotor speed reference. Fig. 8 and Fig. 9 show FLC control and Simplified FLC with 45 rad/s rotor speed reference. The above figures present experimental results for low rotor speed range of FLC control and Simplified FLC control applying load torque. In accordance with the figures above, both control schemes present similar performances in steady state. It is verified that both schemes respond to compensated torque variations. With respect to Simplified FLC, it is necessary to carrefully select fixed gains in order to guarantee the alignment of the rotor flux on the d axis.

**9. Conclusion**

Two different sensorless IM control schemes were proposed and developed based on nonlinear control - FLC Control and Simplified FLC Control. These control schemes are composed of a flux-speed controller, which is derived from a fifth-order IM model. In the implementation of feedback linearization control (FLC), the control algorithm presents a large number of computational requirements. In the simplified FLC scheme, a substitution of FLC currents controllers by two PI controllers is proposed to generate the stator drive voltage. In order to provide the rotor speed for both control schemes, a MRAS algorithm based on reactive power is applied.

To correctly evaluate whether this Simplified FLC does not affect control performance, a comparative experimental analysis of a FLC control and a simplified FLC control is presented. Experimental results in DSP TMS 320F2812 platform show the performance of both systems.
Fig. 4. FLC control with 18 rad/s rotor speed reference
Fig. 5. Simplified FLC control with 18 rad/s rotor speed reference
Fig. 6. FLC control with 36 rad/s rotor speed reference
Fig. 7. Simplified FLC control with 36 rad/s rotor speed reference
Fig. 8. FLC control with 45 rad/s rotor speed reference
Fig. 9. Simplified FLC control with 45 rad/s rotor speed reference
in the 18 rad/s, 36 rad/s and 45 rad/s rotor speed range. Both control schemes present similar performance in steady-state. Hence, the proposed modification of the FLC control allows a simplification of the control algorithm without deterioration in control performance. However, it may necessary to carefully evaluate the gain selection in the simplified FLC control, to guarantee rotor flux alignment on the d axis, as well as, to guarantee speed-flux decoupling. Both control schemes indicate sensitivity with model parameter variation, and one way to overcome this would be the is development of an adaptive FLC control laws on FLC control.

10. References


The subject of this book is an important and diverse field of electric machines and drives. The twelve chapters of the book written by renowned authors, both academics and practitioners, cover a large part of the field of electric machines and drives. Various types of electric machines, including three-phase and single-phase induction machines or doubly fed machines, are addressed. Most of the chapters focus on modern control methods of induction-machine drives, such as vector and direct torque control. Among others, the book addresses sensorless control techniques, modulation strategies, parameter identification, artificial intelligence, operation under harsh or failure conditions, and modelling of electric or magnetic quantities in electric machines. Several chapters give an insight into the problem of minimizing losses in electric machines and increasing the overall energy efficiency of electric drives.

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