Real Time Methods for Wideband Data Processing Based on Surface Acoustic Waves

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1. Introduction

The newly developed methods enjoy the advantages of an optical channel for data transfer (parallel data processing in real time, high operating speed, and noise immunity) and the advantages typical of integrated optics (compactness, low power consumption, high sensitivity in information signal processing, stability against external action, and the possibility of using the batch-fabrication technique). The aforesaid advantages account for the wide use of waveguide acoustooptic (AO) units (WAOU) in computing, fiber-optic, telecommunication, and other photonic systems [1-3]. Conventional WAOUs are constructed from 3D elements. However, size, power consumption, and sensitivity to environmental conditions (vibrations, temperature variations, etc.) set limits on the applications of these devices. The WAOU (typical functional scheme is shown on fig. 1) is based on the waveguide AO Bragg diffraction of the modulated light beam on a modulated surface acoustic wave (SAW) and the registration of this diffraction image. One of the main WAOU parameters is product \( T_A\Delta f \), where \( T_A = W_{opt}/V \) is the maximum delay time, which is known to be equivalent to the propagation time of the SAW leading edge through the optical beams, where \( W_{opt} \) is the optical beam width, \( V \) - the SAW velocity, and \( \Delta f \) is the working frequency band.

The \( x \) axis is directed along the propagation of the optical beam, the \( y \) axis is orthogonal to the waveguide plane and directed to its depth, and the \( z \) coordinate is perpendicular to the direction of propagation of the optical beam.

SAW operates as an optical driving transparency [4,5]. It executes following important operations:
- changing of deflection angle by means of change of SAW frequency (frequency of applied RF-signal) - this property is used for optical deflectors, scanners, switches;
- changing of intensity of diffracted beam by means of change of power of applied RF-signal - this property is used for amplitude modulation;
- changing of frequency of diffracted beam depended on changing of SAW frequency - frequency modulation.

SAW is generated with an electro-acoustical transducer [6]. The transducer type is usual inter digital transducer (IDT).
Fig. 1. Functional scheme WAOU, where $k_0$, $k_1$ – optical wave vectors, $K$ – SAW wave vector, $W(z)$ – optical aperture function, $W_a$ – SAW aperture. Solid lines show optical beams. The source of optical radiation, lens system and registration unit are not shown.

The optical wave passes three areas. The optical wave aperture function $W(z)$ is formed in the first area. This means that the optical wave must be rather wide. There is AO diffraction in the second area. The SAW aperture $W_a$ (is about hundreds $\mu m$) defines the AO diffraction region dimension along the optical beam. This area is situated in a diffused optical waveguide on the lithium niobate crystal surface for the device. There are two optical waves in this area: the undiffracted wave and the diffracted wave. The diffracted wave has the information product of the optical and acoustical signals. The third area realizes two functions: separation diffraction optical beam (from input optical beam) and the AO diffraction image transmission to a CCD array. The separation is obtained on the property that undiffracted and diffracted beams have different propagation angles.

Main purpose. To increase the efficiency of the methods we must use and a proposed make it possible to process both a synthesized optical aperture and a synthesized acoustic aperture.

The problems of theoretical researches, mathematical models, simulation and experimental investigation of the based on Y-cut lithium niobate crystal AO units for real time data processing are discussed.
The propagation of plane optical beams is analyzed in the diffraction approximation with a negligible diffraction distortion (they are quasi parallel) and Fraunhofer approximation [7] is reasonable in this case. So, it is possible to use Fourier transformation for longitudinal optical fields. We suppose that only the TE$_0$ - optical mode exists in a planar optical waveguide. For such a waveguide, we can split the Maxwell equations and consider the time and coordinate components. The analysis of the coordinate components yields a one dimensional mode equation and a two-dimensional wave equation (with effective refractive index $N_{eff}$). For the TE-mode polarisation of guide optical waves the mode Maxwell equation become according to equation [8]:

$$\frac{d^2 E}{d \rho^2} + \left(n^2(\rho) - N_{eff}^2\right) E = 0,$$  \hspace{1cm} (1)

where $\rho = \kappa_0 y$, $\kappa_0$ is the optical wave number, $E$ is optical field distribution normal to the boundary surface of the waveguide, $n(\rho)$ is function of refractive index profile (RIP) normal to the boundary surface of the waveguide. For titanium diffused waveguides the theoretical and experimental research leads us to a profile function for the refractive index given by [9]:

$$n^2(y) = n_s^2 + (n_0^2 - n_s^2)(1 - \alpha)e^{-\left\{\frac{y}{a}\right\}^2} + \alpha e^{-\frac{y}{b}},$$ \hspace{1cm} (2)

where $n_s$ is the substrate refractive index, $n_0$ - is the maximum the refractive index related to Ti-diffusion near the surface, $a$ - is the effective depth of the Ti-profile, $b$ - is the depth of the for out-diffusion, $\alpha$ - is the fraction of the exponential profile. This result was achieved by the optimization of the profile function comparing calculated and measured values of the effective refractive indices for multimode waveguides.

We study the propagation of light in the region of AO interaction assuming that the Bragg diffraction is realized, the properties of the waveguide mode remain unchanged, reflected waves are absent, the amplitude of the diffracted wave slowly increases (we can neglect the second derivation), and the perturbation of the waveguide permittivity caused by the SAW propagation is small [10,11]. The total diffraction losses are insignificant.

The diffraction efficiency of optical beam on SAW submits to the following parity [4,5]:

$$D = A^2(f)\left(\frac{\sin(qW_a)}{q}\right)^2,$$

where $A^2(f) = \Gamma_{00}(f)P_{ac}$ - AO interaction coefficient, $\Gamma_{00}(f)$ - interaction integral for AO diffraction for TE$_{0r}$ TE$_0$ mode regime (the interaction integral for Y-cut lithium niobate crystal was learned in [11, 12], and it’s the frequency dependent is shown on fig. 2a), $f$ - SAW frequency, $P_{ac} = U_{eff}^2 Y_{IDT}$, $U_{eff}$ - IDT supply voltage, $Y_{IDT}$ - IDT radiative transconductive, $q = \left(\frac{\Delta k}{2}\right)^2 + A^2$, $\Delta k$ - disagreement wave vector (see fig. 2b), $W_a$ - IDT aperture.

With allowance for the phase mismatch $\Delta k$ [3], the relation between the amplitude functions of the incident and undiffracted $T_0(x)$ and diffracted $T_1(x)$ optical waves is determined by the solution to the equations of bound modes [10]. Using these assumptions, we can analytically solve the wave equations and derive integral expressions [5].
2. Real time multi-channel time-integrated correlation unit

2.1 Introduction
A classical time-integrated AO correlator (TIAOC) consists of a source of optical radiation (SOR), a collimating objective, an AO cell, an imaging objective, a spatial filter rejecting the null beam, and a CCD array [3, 13]. The main parameters of the AO correlator—the maximum delay time $T_A$. This parameter determines the range of delay times $\Delta T_A$. The input signal $g_{in}(t)$ is used for time modulation of the light beam (for example, internal modulation of a laser or an LED). The second signal $h_{in}(t)$ modulates the amplitude of the acoustic wave with carrier frequency $f_0$. This wave is used for space–time modulation of the transmittance of the acousto-optic cell. The Bragg diffraction angle of the optical beam corresponds to the carrier frequency of the acoustic wave. Since the incident light intensity and the cell transmittance are proportional to $g_{in}(t)$ and $h_{in}(t - z/V)$, respectively, the intensity distribution of the diffracted beam depends on the product $g_{in}(t)h_{in}(t - z/V)$. The cell image is projected on the CCD array, which integrates the intensity distribution with respect to time. The signal from the CCD array yields the spatial distribution of the correlation functions of signals $g_{in}(t)$ and $h_{in}(t)$.

2.2 Mathematical model of a multi-channel WAOU for time-integrated correlation data processing in real time
One method for increasing the integration of the correlation channels is multicolor data processing [14]. In this case, a single device contains $N$ independent correlators. The correlation channels employ optical beams with different wavelengths. This approach facilitates parallel data processing in real time, diminishes the operating costs of an individual acousto-optic correlation channel, and makes it possible to avoid crosstalk and intermode losses.
For the multi-channel TIAOC whose scheme is shown in fig. 3, the input signal $g_{in}(t)$ represents a superposition of $N$ independent optical signals corresponding to different wavelengths $\lambda_m$, where $m = 1...N$. Each optical beam is amplitude modulated. The second input signal $h_{in}(t)$ represents a superposition of $N$ independent electric signals, each of which generates a SAW at the corresponding frequency $f_{in}$ and modulates its amplitude. The value of the carrier frequency is determined from the condition for the maximum in the overlap integral for the AO interaction of the SAW and the corresponding optical beam with a certain wavelength. Each optical beam is diffracted by the corresponding SAW in a waveguide AO Bragg cell (WBAOC). All cells are commoning the own chip. In the far-field region, the total diffracted optical field is a superposition of diffracted optical fields with different wavelengths. A prism is used in the focal plane of the imaging objective to spatially separate the optical beams. Thus, $N$ independent correlation signals are simultaneously detected in the image plane in real time, which means that $N$ independent correlation channels are realized in a single device.

Fig. 3. Functional optical scheme of the multi-channel real time integrated TIAOC: 1 SOR, 2 collimating lenses, 3 WBAOC, 4 image lens objective, 5 CCD array, 6 total correlation function, 7 prism, 8 spatial filter. It’s show two independent channel with different wavelengths. Solid lines show typical paths of optical beams in the device from the SOR to the CCD-array.

With regard to the above conditions, the diffracted field of the $m$th optical wave obeys the following equation:

$$\Delta T_m (x,z) + \left( \frac{2\pi}{\lambda_m} N_{eff} \right)^2 T_m (x,z) = - \int_{-\infty}^{\infty} dy k_{1m}^2 E_0 (y) E_{in}^* (y) T_0_m (x,z)$$  \hspace{1cm} (3)

where $T_0$ and $T_1$ are the longitudinal components of the incident and diffracted waves, respectively. Then, the distribution of the longitudinal component of the $m$-th diffracted optical wave is represented as

$$T_m (x,z,t) = g_{in} (t) \int_0^t d\tau R(z,t,\tau) h_{in} (\tau) ,$$
\[ R(z, t, \tau) = i e^{-i2\pi f_m t} \int df e^{-i2\pi(f-f_0)(t-\tau)} A(\lambda_m, f_0 + f) r(z) e^{\frac{2\pi N_{eff}(W_{wa} + \sin(\frac{\Theta_{wa}}{2}))}{\lambda}} , \]

\[ r(z) = \int d\eta W_{opt}(\eta) \int d\rho e^{-i2\pi(z-\eta)} \sin \frac{\Delta k_m(\rho) W_{wa}}{2} e^{i2\pi(\rho) W_{wa}} , \]

where \( f \) is the modulation frequency.

The optical field outside the waveguide is a 2D field, whose transverse size is mainly determined by the quantity \( W_{opt} \) and the diffraction broadening. In the first approximation, we can neglect the diffraction broadening of the beam, since its angular divergence is about 0.1x10^-2 rad. The vertical size of the field depends on the ratio \( \lambda/n_{sub} \). For the TE_0 mode, the field distribution along the vertical axis determined by (1) is close to the Gaussian distribution. Therefore, all effects are concentrated in the transverse cross section of the optical field. This makes it possible to analyze the propagation of light in the correlator under study in the one-dimensional approximation.

For known parameters of the imaging objective, the intensity distribution for the \( m \)th correlation channel in the image plane is given by

\[ I_m(z) = \frac{1}{\sqrt{2T_{int} R_{mag} \sigma}} \int_{-\infty}^{\infty} dt \int_{-\infty}^{\infty} d\xi I_{WBAOC_m}(t_{in} + t_{out} t_{s} e^{-\frac{\xi + \Delta z}{\sigma}} z, \frac{\Delta x}{R_{mag}})^2 , \]

where \( R_{mag} \) is the magnification of the imaging objective, \( T_{int} \) is time integrated, \( \sigma \) is the resolution of the imaging objective, and \( I_{WBAOC_m} \) is the integral intensity of the diffracted light for a \( m \)-th correlation channel, \( t_{in}, t_{out} \) are the translate coefficients of the prisms providing the chip incoupling/outcoupling of optical radiation, \( t_{s} \) is the translate coefficient of the prism providing the separation of optical radiation.

### 2.3 Computer simulation results

Using the model proposed, we theoretically analyze the values of the physical parameters of a hybrid five channel TIAOC. The WAOC consists of five WAOBCs that serve as a time optical transparency. The lens system of the correlator is made up of volume objective lenses [15]. For the numerical calculations, we use the following parameters. The effective depths of the refractive index profile are 2.24 and 6.52 \( \mu m \) and \( \Delta n^2 = 0.005 \). The SAW velocity is 3488 m/s. Using these parameters, we perform computer simulation to optimize the IDT structure for each correlation channel. The value of the rectangular optical aperture function is \( W_{opt} = 7 \) mm. The resulting field is a superposition of independent optical fields corresponding to individual correlation channels. The spatial separation depends on the optical properties and configuration of the prism. The aperture and the focal length of the imaging objective are 120 and 16 mm, respectively. The magnification is \( R_{mag} = 1/16 \). Both input modulating signals are rectangular signals of equal duration. The computer simulation results predict complete separation of the diffracted and undiffracted optical beams in the focal plane of the imaging objective.

At the given values of the physical parameters, we numerically study the characteristics of a hybrid five channel TIAOC. The table 1 shows the main parameters of this device. Figure 4
demonstrates the results of the computer simulation of the diffraction patterns in the correlator image plane for various durations of the input signals. In the case under consideration, the total correlation function consists of five parts.

<table>
<thead>
<tr>
<th>Parameters/correlation channel</th>
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<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
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<td>0,88</td>
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<td>2</td>
<td>2</td>
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<td>3. IDT parameters</td>
<td></td>
<td></td>
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<td></td>
<td></td>
</tr>
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<td>3.1. Central carrier frequency $f_0$, MHz</td>
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<td>321</td>
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<td>436</td>
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<td>1,2</td>
<td>1,3</td>
<td>1,5</td>
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<td>3.3. Frequency bandwidth, MHz</td>
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<td>15</td>
<td>16</td>
<td>16</td>
<td>18</td>
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<td>3.4. Aperture, µm</td>
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<td>400</td>
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<td>450</td>
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<td>3.5. Number of the fingers</td>
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<td>49</td>
<td>47</td>
<td>41</td>
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<tr>
<td>3.5. Voltage standing-wave ratio in the working frequency range</td>
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<td>1,2</td>
<td>1,2</td>
<td>1,2</td>
<td>1,2</td>
</tr>
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<td>5. Minimum power of the RF signal, mW</td>
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<td>70</td>
<td>60</td>
<td>50</td>
<td>50</td>
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<tr>
<td>6. Minimum power of the optical signal, mkW</td>
<td>0,22</td>
<td>0,19</td>
<td>0,17</td>
<td>0,15</td>
<td>0,15</td>
</tr>
</tbody>
</table>

Table 1.

The maximum number of independent TIAOCs employing WAOCs based on the $Y$-cut lithium niobate substrate is 100.

![Fig. 4. Total correlation output signals for various durations of the input signals: from $T_A$ to $0.05T_A$ (the delay time of $g_{in}(t)$ relative to $h_{in}(t)$ is $0.5T_A$). The families of curves correspond to the first (left-hand) to fives (right-hand) correlation channels, respectively.](www.intechopen.com)
Using a mathematical model of the multi-channel TIAOC, one can also numerically analyze the characteristics of a hybrid monochrome TIAOC, in particular, at relatively small SAW variations. The validity of such an approach follows from the comparative analysis of the theoretical and experimental data. We employ an experimental prototype whose structure is described in detail in [16]. For the numerical calculations, we assume that, as in [16], WAOC contains a single WBAOC and two prisms providing the incoupling and outcoupling of optical radiation. The numerical experiments are performed for the wavelength in a vacuum \( \lambda_0 = 0.78 \) \( \mu m \), the SAW velocity \( V = 3488 \) m/s, and an optical aperture function whose value is 7 mm. The remaining initial data correspond to the experimental sample from [16]. Figure 5a demonstrates the results of the computer simulation and experimental data on the dependences of the normalized correlation peak height on the duration of the input signals at their relative duration of 0.5 \( T_A \). The experimental peak value is determined relative to the optical signal that is generated at the output of the device in the steady-state mode. The numerically calculated results can be presented in a similar way. Note also that the contributions related to additional biases applied to the optical source and WBAOC (pedestal contributions) are not taken into account in the results of the numerical calculations and experimental data.

Fig. 5. (a) Plots of the normalized correlation peak height (\( J_{p, \text{norm}} \)) vs. duration (in fractions of \( T_A \)) of input signals at a relative delay of 0.5\( T_A \): (1) rectangular optical aperture function, (2) experimental optical aperture function, (3) experimental data from [16], and (triangles) experimental points. (b) Experimental optical aperture function.

Based on the comparative analysis of the numerical and experimental data, we draw the following conclusion. The proposed mathematical model can be used to analyze the affect of variations in the SAW velocity on the correlation signal, since both dependences are linear. However, the slope of the calculated curve differs from the slope of the experimental curve. This is due to the fact that the shape of the experimental aperture function significantly differs from the rectangular shape. The real shape is important in the calculation of the parameters of the given TIAOC. For comparison, Fig. 5a shows similar results calculated with allowance for the shape of the aperture function used in the experiments (Fig. 5b). In this case, the slopes are virtually identical.
2.4 Conclusion
We propose an AO method for time-integrated multi-channel correlation data processing in real time. This method enables one to significantly increase the number of independent correlation channels. We develop a mathematical model of a multicolor AO device for real-time correlation analysis with time integration. We theoretically and numerically analyze the characteristics of a hybrid five channel correlator, whose AO chip is based on the Y-cut lithium niobate substrate. Multi-channel AO correlators with time integration make it possible to simultaneously detect up to 100 correlation functions provided that Y-cut lithium niobate serves as the substrate.

3. Bandwidth AO unit for the real-time spectrum analysis of optical signals
3.1 Introduction
The design and development original AO method for the real-time spectral analysis of broadband optical signals are discussed. The unit implemented this mean allows for the real-time processing of an optical signal that exhibits a complicated spectrum with hundreds of components. This unit may also serve as a high-accuracy real-time optical-frequency detector working in a wide spectral range.

Figure 6 shows that the classical AO unit consists of three components: optical port (1), waveguide AO chip (2), and photodetector unit (3). The optical signal from the first unit is fed to the WAOAC, where it is collimated with an aplanatic lens (4) to a wide-aperture plane wave (5). Then, the wave propagates through the region of the perturbed planar waveguide (6), which is induced by the propagating surface acoustic wave (7) generated by an electroacoustic IDT (8). In this case, the Rayleigh SAW with strictly fixed frequency \( f_0 \) serves as an optical transparency. Then, a component of the optical signal is deflected due to Bragg diffraction by the angle [10]

\[
\Theta_m = \frac{\lambda_m}{V} f_0 ,
\]

where \( \lambda_m \) is the radiation wavelength of the \( m \)-th component in the waveguide.

The number of the diffracted optical beams corresponds to the number of the frequency components of the original optical signal. The resulting diffraction field is focused with an aplanatic lens (9) on the end of the waveguide and is detected with a photodetector array (3).

The mathematical model of the waveguide AO spectrum analyzer of the optical radiation is similar to the well-developed and experimentally tested model of the waveguide AO spectrum analyzer of radio signals [16]. The differences are as follows: first, the parameter under study is the radiation wavelength rather than the radio frequency (which is fixed); second, the chromatic dependence of the overlap integral of the Bragg AO interaction needs to be taken into account.

The optical wave diffracts on SAW. Thus the diffraction efficiency of each optical component submits to the following parity:

\[
D = A^2(\lambda_m, f_0)\left(\frac{\sin(q_m W_d)}{q_m}\right)^2,
\]
where \( A^2(\lambda_m, f_0) = \Gamma_{00}(\lambda_m) p_{ac} \) - AO interaction coefficient for m-th optical component, 
\( \Gamma_{00}(\lambda_m) \) - chromatic interaction integral for AO diffraction for \( TE_0 \) - \( TE_0 \) mode regime,
\( q_m = \left( \frac{\Delta k_m}{2} \right)^2 + A^2(\lambda_m, f_0) \), \( \Delta k_m \) - disagreement wave vector for corresponding optical component.

The frequency of a everyone diffracted optical beam will be moved on frequency \( f_0 \). And the quantity of diffracted optical beams corresponds to quantity of frequency components of an initial signal.

In general, the band of the working optical frequencies is bounded by the SAW excitation band, the AO interaction band, the frequency band of the overlap integral, which characterizes the AO properties of the material, and the band of the optical frequencies in which the planar waveguide supports a single \( TE_0 \) mode. The last two parameters are significantly more important than the first two parameters. A single IDT is insufficient for the analysis of the broadband optical signals, since the band of the analyzed optical frequencies is relatively narrow (about 100 nm) [4, 5]. In contrast to the monochromatic case, the characteristic is strongly asymmetric, since the overlap integral decreases with increasing wavelength at relatively large \( \Delta \lambda \). For this reason, a multiple-IDT system is used to increase the width of the frequency band. In this system, the crossed structure of acoustic beams enables one to maximize the diffraction efficiency. Several IDTs that excite SAW are placed at the Bragg angle relative to the propagation direction of the channeled radiation. The complexity of this scheme lies in the manifestation of the interference effects for the optical beams diffracted by different SAW beams. This leads to a significant nonuniformity of the frequency characteristic. To solve this problem, we need to employ computer simulation for the amplitude and phase tuning of the device (both the topological parameters of the cell and the electric circuit for the matching of the IDT and RF systems are tuned). It is demonstrated in [5] that the amplitude and phase matching is stable only for three IDT’s.
3.2 Mathematical model of AO units for the real-time spectrum analysis of bandwidth optical signals

In case greatest possible value (~300 nm) of a bandwidth of an optical signal (such signals can propagated in waveguide at only $TE_0$-mode regime) use 3 ITD obviously insufficiently. One of ways of increase of a optical frequency bandwidth is entering an additional mismatch of wave vectors with the purpose of increase of a total optical frequency bandwidth, but as the consequence is observed decrease of diffraction efficiency. This approach is realised by change of value of a angle between an optical beam and SAW front, that is achieved additional turn of the ITD. Thus should be satisfied condition:

$$\frac{\sin(q_iW_n)}{q_i} = \left[ \frac{\pi}{2} (4n + 1) \right]^{1/2},$$

(8)

where $n=0, 1, 2, 3$.

Thus the diffraction efficiency of a each optical component submits to a parity (7). The regime of low diffraction efficiency allows to simplify parities describing optical fields:

$$T_0 = \text{const}$$

$$T_1 = -i \frac{A(\lambda_m)T_0}{\Delta k} e^{-i(\Delta k x + \Phi(z))},$$

(9)

where $T_0$ - longitudinal initial optical field component, $T_1$ - longitudinal diffracted optical field component, $\Phi(z)$ - phase of longitudinal diffracted optical field component [4,5].

The optical field each wave components is the sum an optical field generated appropriate SAW, extending under different angles to an initial optical beam. Presence several coherent the optical field results in them interference. Then the optical field separate wave components under condition of low efficiency diffraction submits to the following parity:

$$T_{1n}(x) = -i \frac{A(\lambda_m)T_0}{\Delta k_1} e^{-i(\Delta k_{1x} + \Phi_1(z))} \left( 1 + \sum_{j=2}^{N} \frac{\Delta k_j}{\Delta k_1} e^{-i((\Delta k_{1x} - \Delta k_j)x + (\Phi_1(z) - \Phi_1(z) + \Phi_1(\psi)))} \right).$$

(10)

The given field by means of an integrating lens is transferred on a ruler of photoreceivers placed in a lens focal plane. The intensity distribution of each wave component in a focal plane of an integrating lens is described by parity [17]:

$$W_{I_m}(x_0, z) = \int_{-\infty}^{\infty} d\xi \frac{(1 + \phi)}{\sqrt{s}} T_{1n}(\xi, \eta) e^{-i(\Phi_2(z) + k_N \psi \cos(\psi))},$$

(11)

where $s$ - the distance from the point on last lens contour to the observation point, $\phi$ - the angle between the ray coming to the point $\xi$ to point $(x_0, z)$, $\psi$ - the angle between the phase and group velocity for the ray directed towards the observation point, $\Phi_2(z)$ - the phase of optical ray at the point $\xi$.

The total optical field is superposition of fields a each optical component.

An increase in the aperture function leads to an additional decrease in the sensitivity of the frequency characteristic to the interference effects. This is due to the averaging of the phases.
of the diffracted beams. It follows from the analysis of the phase dependences of the interfering beams that the interference effects are completely eliminated provided that the optical aperture satisfies the following condition:

$$W_{\text{opt}} \gg \frac{\Delta \lambda}{4\Delta \Theta^2}$$

(12)

where $\Delta \lambda$ is the wavelength band of the analyzed radiation and $\Delta \Theta$ is the difference between the Bragg angles of the neighboring IDT’s. For the typical parameters $\Delta \lambda = 100$ nm and $\Delta \Theta =0.0017$, condition (12) is satisfied for an optical aperture of about 100 mm. However, such large apertures cannot be technically realized in the integrated optical devices, and the aforementioned property provides for only partial compensation of the interference effects.

3.3 Computer simulation results

We develop two modifications of the AO devices for the spectral analysis of the red and IR broadband optical signals. In these devices are based on $Y$-cut lithium niobate. The refractive index profile of diffusion planar optical waveguide is described the following parameters. For the first modification, the effective depths are 2.24 and 6.52 mkm and $\Delta n^2 = 0.005$. For the second modification, the effective depths are 2.42 and 6.12 mkm and $\Delta n^2 = 0.008$. TIPE technology [18] is used to fabricate aplanatic lenses. We assume that the optical aperture function is nearly Gaussian and its values for the first and second modifications are $W_{\text{opt}} = 5$ and 7 mm, respectively. The SAW velocity is 3488 m/s. Based on these parameters, we employ computer simulation to optimize (i) the IDT-system design with respect to the maximization of the band of the analyzed optical frequencies and (ii) the topology of the lens system with respect to the maximization of the optical resolution using the method proposed in [19]. The table 2 demonstrates the main parameters of the two modifications obtained with the numerical and experimental study.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Mod. 1</th>
<th>Mod. 2</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>simul.</td>
<td>exper. [16]</td>
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<tr>
<td>1 Optical radiation waveguide range</td>
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<tr>
<td>- low wavelength, nm,</td>
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<td>- high wavelength, nm,</td>
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<td>2 Working wavelength band, nm</td>
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<td>3 Resolution of two optical wavelengths, nm,</td>
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<td>4 Measuring fixed frequency for RF signal, MHz</td>
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<td>5 Diffraction efficiency, %/W</td>
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<td>6 Dynamic range, dB</td>
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<td>0.4</td>
<td>0.6</td>
</tr>
<tr>
<td>9 Voltage standing wave ratio for driving RF signal</td>
<td>1.8</td>
<td>2</td>
</tr>
</tbody>
</table>

Table 2.
Figure 7a shows the numerically calculated dependence of the optical transmittance of the first modification on the wavelength. At a level of -3 dB, the working wavelength band is slightly greater than 335 nm in the range from 935 to 600 nm. For comparison, we also present the experimental characteristic of this AO device from [16]. Figure 7b shows the wavelength dependence of the calculated optical transmittance for the second modification. At a level of -3 dB, the working wavelength band is 360 nm in the range from 1125 to 765 nm. Note that the parameters of the device are chosen with allowance for the technological requirements for its fabrication. A working band of 360 nm is the ultimate band for the single mode diffusion waveguides under study [14]. The optical signals with such maximum bandwidth can be supported with the waveguides under study in the IR range.

Fig. 7. Plots of optical transmittance $D$ vs. wavelength for (a) the first modification of the spectrum analyzer, (b) for the second modification of the spectrum analyzer.

The comparative analysis yields a good agreement between the theoretical and experimental data on the first modification. In particular, the difference between the RF signals is less than 1%, the difference between the central optical frequencies is almost 10%, and the difference between the working transmission bands is less than 10%.

Figure 8 demonstrates the experimentally determined accuracy of the measurement of the optical signal wavelength with the first modification in which a laser diode serves as the source of the optical signal.

The left panel shows the typical response of the device. At a fixed frequency of the RF signal and a stable radiation of the laser diode, the response is symmetric (Fig. 8a). A variation in the input current of the laser diode leads to a variation in the radiation wavelength, which causes a variation in the response (Fig. 8b). In this case, the voltage difference between the Nth and $(N + 1)$th pixels is 0.2 V. The response can be symmetrized by tuning the oscillator frequency. The difference between the oscillator frequencies is 38 kHz. Thus, the wavelength of the laser diode is varied by 0.054 nm. In practice, we can observe and measure a voltage difference of about 10 mV between the $(N - 1)$th and $(N + 1)$th pixels. Hence, the ultimate accuracy of the wavelength measurement for the optical signal in the device under study is no worse than 0.01 nm.
3.4 Conclusion
We developed and numerically studied two modifications of the AO device for the spectral analysis of broadband red and IR optical signals. We employ a mathematical model which is similar to the experimentally tested mathematical model of the waveguide AO analyzer of radio signals. The comparative analysis yields a good agreement between the theoretical and experimental results. The band of the working optical frequencies is 360 nm in the range 765–1125 nm. The wavelength resolution of the two optical signals determined with the Rayleigh criterion is 3 nm. The optical wavelength is measured with an accuracy of 0.01 nm. The minimum level of the analyzed optical signal is 10 mkW. In particular, the differences between the RF signals, the central optical frequencies, and the working transmission bands are less than 1%, almost 10%, and less than 10%, respectively. The parameters of the device are chosen based on the real technological and topological requirements for its elements.

4. Methods for real-time optical scanning of large data arrays

4.1 Introduction
A distinctive feature of the methods proposed is a significant increase in the number of scanning points (information bits) in comparison to the classical method involving spectral analysis of broadband RF signals based on waveguide AO Bragg interaction [4, 16]. In a conventional scanning system, the frequency of the controlling RF signal fed to a scanning unit is discretely varied within the frequency band of the device. A variation in frequency leads to a variation in the diffraction angle of the optical beam [10]:

$$
\Theta_{dif} = \Theta_o + \arcsin\left(\frac{\lambda_{o,f}}{N_{eff}V} - \sin\Theta_a\right)
$$

(13)

where $\Theta_o$ is the angle between the fronts of the optical beam and surface acoustic wave, and $\Theta_a$ is the angle between the SAW propagation direction and the $z$ axis.
A variation in the diffraction angle causes a shift of the focused optical beam to the neighboring point in the focal plane coinciding with the side surface of the waveguide. The
scanning is thus realized. The discrete step in the frequency variation depends on the frequency resolution of the optical focusing system [4]. The number of scanning points is given by

\[ N_T = \frac{\Delta f}{R_f} \]  

(14)

where \( \Delta f \) is the frequency band and \( R_f \) is the resolution of the focusing optical system.

The hardware for realizing the above method employs a source of optical radiation and a waveguide acoustooptic chip. The chip contains a planar optical waveguide, optical input/output elements, an optical system consisting of collimating and focusing lenses, and a waveguide AO Bragg cell. Note that for scanner elements based on Y-cut lithium niobate, the number of scanning points is no greater than 1000 for the ultimate values of \( \Delta f \) and \( R_f \) [4]. However, the technical realization of such a device is difficult and expensive [16].

### 4.2 Method for one-dimensional scanning

A conventional method for 1D scanning can be improved to achieve a significant increase in the amount of data processed in real time using an approach that employs a synthesized (with a few optical beams) aperture of the optical field. The total information field is divided into subareas, each of which is irradiated with an individual optical beam controlled by the corresponding WAOBC. In the case under consideration, the first optical beam is incident on the corresponding cell at an angle \( \Theta_{\text{max}} \) equal to a double Bragg angle corresponding to the upper bound limit of the cell working frequency range. The next optical beam is incident on the second WAOBC at an angle \( \Theta_{\text{max}} + \Delta \Theta_c \), where \( \Delta \Theta_c \) is the working range of angles of the previous cell. In the general case, the angle of incidence of the current optical beam differs from the previous one by \( \Delta \Theta_c \). (Fig. 9). Thus, the scanning range increases by a factor of \( M \), where \( M \) is the number of cells.

A similar WAOBC system is placed symmetrically with respect to the optical axis. Note the matching of the working range of angles of the focusing system (\( \Theta_L \)) and the total working range of the WAOBC system. Hence, the number \( M \) satisfies the following condition:

\[ M < \frac{\Theta_L}{2\Delta \Theta_c} \]  

(15)

Thus, the total number of scanning points is given by

\[ N_{T_{\text{total}}} = 2MN_T \]  

(16)

We investigate the propagation of a monochromatic coherent quasi-plane optical wave with a predetermined aperture function \( W(z) \). We assume that the AO Bragg phase matching condition [5] is satisfied, the diffraction efficiency is about a few percent. In the general case, the aperture of the surface acoustic field is synthesized with a few electroacoustic IDTs.

In the far-field zone, the electrical component of optical field diffracted by each WAOBC is represented as

\[ T_1(x,z,t) = T_0(x) \int_{-\infty}^{\infty} dk \sum_{j=1}^{N} \frac{A \theta(f)}{k(x,z)} e^{i2k\theta x} \left( 1 - e^{-i\omega(t-T_0)-N \phi(f)(\sqrt{k^2-k^2_{\text{c}}})x + \theta(f)} \right) e^{-\alpha(f)z} \]  

(17)
where \( \omega \) and \( k_0 \) are the frequency and wave number of the \( TE_0 \) mode; \( \Omega \) and \( K \) are the frequency and wave number of the SAW; \( A_b(f) \) is the Bragg AO interaction coefficient corresponding to parameter \( A(f) \), determined in sec. 1., \( N \) is the number of IDTs; \( W_a \) is the \( j \)-th IDT aperture; \( \Phi_B(x, z, f) \) is the phase related to the RF electric signal passing through the matching electric circuit, SAW propagation from the electroacoustic transducer to the region of acoustooptic interaction, and interference depending on the acoustic field topology [5, 11]; and \( \alpha(f) \) is the SAW decay coefficient, which was analyzed in detail in [6]. This field is focused using a waveguide lens objective with focal length \( F \). In the back focal plane of the objective, the field distribution is represented as

\[
W_F(x, z) = \int_0^{T_{Sc}} \int_{-\infty}^{\infty} d\tau d\xi \frac{1 + \phi}{\sqrt{s}} T_1(\xi, \eta, \tau) e^{-i(\Phi_2(x) + k_b N_c (\nu) s \cos(\nu))} \tag{18}
\]

where \( T_{Sc} \) is the scanning time.
4.3 Computer simulation results
Using the above approach, we developed a AO planar scanning device based on Y-cut lithium niobate. This device makes it possible to selectively process more than 3000 information bits in real time. The device consists of four WAOBCs (two cells on each side of the optical axis). It is possible to arbitrarily control the cells. Using the model proposed, we numerically study the characteristics of this scanner working in real time. In numerical experiments, we employ the following typical initial data presented in the table 3. The aperture function of the optical beam is nearly Gaussian, and the corresponding value is $W_{opt} = 5$ mm.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Planar waveguide</td>
<td></td>
</tr>
<tr>
<td>Effective refractive index for TE$_{0}$ mode</td>
<td>2.19176</td>
</tr>
<tr>
<td>Difference between maximum refractive indices of the waveguide and substrate</td>
<td>0.8x10$^{-2}$</td>
</tr>
<tr>
<td>Depth of the Gaussian profile, $\mu$m</td>
<td>2.42</td>
</tr>
<tr>
<td>WAOBC parameters</td>
<td></td>
</tr>
<tr>
<td>Total working frequency range at a level of 3 dB, MHz</td>
<td>1090</td>
</tr>
<tr>
<td>Range of diffraction angles, rad</td>
<td>0.111</td>
</tr>
<tr>
<td>Maximum diffraction efficiency, %/W</td>
<td>0.97</td>
</tr>
<tr>
<td>Number of sections in the first IDT</td>
<td>17</td>
</tr>
<tr>
<td>Aperture of the first IDT, $\mu$m</td>
<td>450</td>
</tr>
<tr>
<td>Number of sections in the second IDT</td>
<td>23</td>
</tr>
<tr>
<td>Aperture of the second IDT, $\mu$m</td>
<td>280</td>
</tr>
<tr>
<td>Electric power of the RF signal, W</td>
<td>0.6</td>
</tr>
<tr>
<td>Voltage standing-wave ratio in the working frequency range</td>
<td>less than 2</td>
</tr>
<tr>
<td>Parameters of the optical lens system</td>
<td></td>
</tr>
<tr>
<td>Difference between maximum refractive indices of the TIPE lens and substrate</td>
<td></td>
</tr>
<tr>
<td>Effective depth of the TIPE lens, $\mu$m</td>
<td>0.0328</td>
</tr>
<tr>
<td>Focal length of the collimating system, mm</td>
<td>4.24</td>
</tr>
<tr>
<td>Number of lenses of the focusing objective</td>
<td>2</td>
</tr>
<tr>
<td>Focal length of the focusing objective, mm</td>
<td>35</td>
</tr>
<tr>
<td>Aperture of the focusing objective, mm</td>
<td>15.8</td>
</tr>
<tr>
<td>Size of the scanning optical spot, mkm</td>
<td>0.22</td>
</tr>
<tr>
<td>Main characteristics of the WAOC</td>
<td></td>
</tr>
<tr>
<td>Number of WAOBCs</td>
<td>4</td>
</tr>
<tr>
<td>Aperture of the optical beam, mm</td>
<td>5</td>
</tr>
<tr>
<td>Angle between the optical axis and the optical beam for the first WAOBC, rad</td>
<td>0.130</td>
</tr>
<tr>
<td>Angle between the optical axis and the optical beam for the second WAOBC, rad</td>
<td>0.240</td>
</tr>
<tr>
<td>Total number of scanning points</td>
<td>4360</td>
</tr>
</tbody>
</table>

Table 3.
Based on these parameters, we employ computer simulation to optimize the IDT system of the WAOBC. The system consists of two fan IDTs [20] spanning the following frequency ranges: 230–720 and 720–1320 MHz. Figure 10 shows the frequency characteristic of the WAOBC. The elements transforming the aperture function of the optical beam are manufactured using TITE technology [19]. The topology and parameters of the lens system are determined by (i) the ratio of effective refractive indices outside and inside the lens with regard to the aberration of optical beams with large angular aperture, (ii) condition (15), (iii) the optical beam aperture, and (iv) the size of the substrate. With allowance for all these characteristics and a substrate length of 80 mm, we use computer simulation to optimize the topological parameters of the scanning device. The table lists the results of optimization. The maximum allowed frequency resolution $R_f$ of Gaussian optical beams with a 5-mm aperture equals 1 MHz [19]. Then, the number of points scanned in real time using the device under consideration is 4360. The size of the scanning optical spot (0.22 µm) is close to the diffraction limit.

![Figure 10. Frequency characteristic of the WAOBC](image.png)

### 4.4 Method for 2D scanning

We can realize 2D optical scanning simultaneously using two types of waveguide AO diffraction (Bragg (coplanar) and radiative (collinear)) [21]. Figure 11 gives a functional scheme of the 2D scanning device taking into account the aforementioned results. In the case under consideration, the waveguide mode of TE$_0$ polarization propagating in the WAOC from the corresponding SOR to the scanning plane is transformed in the following manner. First, the collimating system (not shown in Fig. 11) forms a wide-aperture optical beam. Then, the beam propagating through the WAOBC is diffracted by a SAW under Bragg conditions. The diffracted optical beam is deflected from the initial direction by the double Bragg angle (see expression (13)). In the case of radiative diffraction, this beam is deflected into the substrate owing to the interaction with a collinearly propagating SAW. The angle at which the optical beam is re-emitted into the substrate is given by [10]
Fig. 11. Functional scheme of the AO scanning device for processing of 2D data arrays: (1) WAOC, (2) WAOBC, (3) IDT, (4) volume focusing lens objective, and (5) total information field. Solid lines show typical paths of optical beams in the waveguide and to the scanning plane. Dashed lines show the trajectories of optical beams re-emitted into the substrate.

$$\Theta_{rd} = \arccos \frac{N_{eff} - \frac{\lambda_0 f}{V}}{n_{sub}},$$

(19)

where $\Theta_{rd}$ is the angle between the guided mode and the mode of radiation and $n_{sub}$ is the refractive index of the substrate. Then, separation of the optical beams takes place. A doubly diffracted optical beam is projected onto the scanning plane using a volume lens objective. Non diffracted and singly diffracted optical beams are rejected with a spatial filter. A variation in the working frequencies of the IDT system placed at a Bragg angle relative to the $z$ axis and IDT placed at a mean Bragg angle relative to the $x$ axis leads to 2D motion of the doubly diffracted optical beam on the screen. We analyze the propagation of light in a single mode planar waveguide with simultaneous application of two types of AO interaction using approximations similar to those mentioned above. Then, the diffraction field of a forward optical wave at a certain cross section is given by the following system of equations:

$$\frac{dT_0(x)}{dx} = iA_0T_1(x)e^{-i(\Delta_k x - \Phi_i)},$$
\[ \frac{dT_1(x)}{dx} = iA_BT_0(x)e^{i(\Delta k_x x - \Phi_0)} \]
\[ \frac{dT_1(x)}{dx} = i\frac{1}{(1 - 2\beta)x}A_{rd}T_2(x)e^{-(i\Delta k_x x + \alpha)} \]  
\[ \frac{dT_2(x)}{dx} = i\frac{1}{(1 - 2\beta)x}A_{rd}T_1(x)e^{(i\Delta k_x x - \alpha)} \]  

(20)

where \( T_2(x) \) is the amplitude function of a doubly diffracted optical wave, \( \alpha \) is the sum of decay coefficients of the optical beam and the collinearly propagating SAW, \( \beta \) is the diffraction divergence coefficient of the collinearly propagating SAW, \( A_{rd} \) is the efficiency of radiative AO interaction, which similar to coefficient \( A(f) \), where the parameter \( \Gamma_{00} \) is replace of the factor \( \Gamma_{rd} \), and \( \Gamma_{rd} \) is the overlap integral for TE\( _0 \)–TM\( _{sub} \) diffraction.

For an arbitrary RIP of a waveguide, the solution to this system of equations can be found only using numerical methods under the following initial conditions: \( T_0(0) = 1 \) and \( T_1(0) = T_2(0) = 0 \). Note that, in contrast to the Bragg case, the frequency characteristic of radiative diffraction exhibits a strong nonuniformity owing to interference effects related to the finiteness of the spectrum of the radiation mode.

4.5 Computer simulation of characteristic of the AO unit for 2D scanning

In the part of the approach proposed, we developed an AO unit for 2D scanning whose WAOC is based on Y-cut lithium niobate. For numerical experiments, we choose similar initial data. The optical aperture function is \( W_{opt} = 3 \) mm. We employ the same WAOBC. Based on these parameters, we use computer simulation to optimize an IDT generating a SAW that propagates collinearly to the optical beam. The parameters of the SAW are as follows: central frequency, 571 MHz; frequency range, 523–635 MHz; IDT aperture, 3100 \( \mu \)m; metallization coefficient, 0.51; and voltage standing-wave ratio, no greater than 2 in the entire frequency range of the IDT. Based on the deflection of each diffracted optical beam, the angles of IDTs relative to the \( x \) axis are -0.24, -0.13, 0.13, and 0.24 rad. Figure 12 shows the results of computer simulation of the resulting frequency characteristic for a single 2D AO scanning channel at a radiative AO interaction length \( L_{a-o} = 2.5 \) cm. In the case under consideration, for an electric power of the control RF signals of 0.5 W, the maximum diffraction efficiency is 0.3%. In accordance with the Rayleigh criterion, the number of resolved states is 650 points on the vertical axis and 650 points on the horizontal axis. The total information field is then 2600 x 650 points (information bits).

4.6 Conclusion

We analyze original methods for real-time optical scanning of large data arrays based on waveguide AO Bragg interaction with a synthesized optical aperture using a few optical beams. The methods proposed make it possible to process both one- and 2D data arrays. A distinctive feature of the methods is an increase in the number of scanning points in comparison to the classical method involving spectral analysis of broadband RF signals based on waveguide AO Bragg interaction. We developed a mathematical model of a waveguide AO scanning device with a large number of based on Y-cut lithium niobate, the
Fig. 12. Frequency characteristic of a single 2D scanning channel: right, left, and cross hatching correspond to the ranges -2-3, -1-2, 0-1 dB, respectively.

number of points for real-time 1D scanning is 4360. There exist two factors accounting for the practical importance of the mathematical model proposed in this work. First, the mathematical model is based on the experimentally tested mathematical model of a waveguide AO spectrum analyzer. Second, we choose the parameters of the device based on real technological and topological requirements for its elements. Note that all the elements of the AO scanning device (except for SOR) can be realized for a single substrate. Using the method for 1D scanning, we developed a mathematical model of a WAOU for real-time 2D scanning. We perform computer simulation of its characteristics for Y-cut lithium niobate. The number of points for real-time scanning is 650 on the vertical axis and 2600 on the horizontal axis. The parameters of the IDT generating a collinear SAW are calculated under the same conditions as the parameters of the IDT in a WAOBC. The aforesaid facts make it possible to conclude that the model proposed can be applied in practice.

5. Saw velocity fluctuation effects

5.1 Introduction
In the development of waveguide AO devices for data processing, one must analyze the accuracy level in the reproduction of the predetermined characteristics. For example, if an AO device is designed based on a certain value of the surface acoustic wave velocity $V_0$ and a real value of velocity $V_1$ differs from this value owing to several factors, the characteristics are changed. In practice, multiple mechanisms lead to a variation in the physical properties of the substrate material, which, in turn, causes variations in the SAW velocity [6]. The most typical mechanisms are related to the ambient temperature, the ionization effect, and the spread of velocities due to errors in the crystal orientation. Note that we consider the case in
which the external action does not result in mechanical variations in the components of devices.

We numerically study the characteristics of two basic AO devices for real-time information processing: time-integrating correlator and broadband spectrum analyzer (AOSA) of radio signals. Both devices are based on a waveguide AO chip that is fabricated on a Y-cut lithium niobate substrate.

5.2 Mathematic model

We analyze the scenarios in which the deviation of the SAW velocity from the calculated value is small, so that the relative variation in the velocity is several percent. In this approximation, we assume that, in the range under study, the SAW velocity exhibits a linear dependence on a certain factor. This assumption is in agreement with the experimental data from [1]. Then, such a dependence can be represented as [22]

\[ V_1 = \chi V_0 = (1 - \frac{\Delta V}{V_0})V_0, \]  

where \( \chi = 1 - \frac{\Delta V}{V_0} \), and \( \Delta V = V_0 - V_1 \) is a variation in the SAW velocity. Parameter \( \chi \) can be physically interpreted as a coefficient of the SAW velocity fluctuations. Note that, in the case under study, this coefficient is constant.

Morgan proposes studying the effect of a minor degradation of the SAW velocity on the characteristics of the device using the model of a linear source and a linear receiver located at a free crystal surface [22]. He also assumes that the diffraction, propagation loss, and SAW dispersion can be neglected in the analysis. For distance \( l \) between the source and the receiver, the calculated time delay is \( t_0 = \frac{1}{V_0} \), whereas \( t_1 = \frac{1}{V_1} \) is the time delay that corresponds to a certain level of the effect of one of the degradation mechanisms. The relationship between these delays is given by

\[ t_1 = \frac{1}{\chi} t_0, \]  

This causes a variation in the time scale of the pulse response of the electroacoustic IDT, which is described with functions \( h_0(t) \) and \( h_1(t) \) at the SAW velocities \( V_0 \) and \( V_1 \), respectively. The relationship between the pulse responses is represented as \( h_1(t) = h_0(\chi t) \).

We assume that the pulse responses correspond to the short-circuiting mode, so that the effect of the external action on the matching circuits is eliminated. It is demonstrated in [22] with neglect of minor variations in the amplitude that the frequency response functions of the device exhibit frequency rescaling with a factor of \( \frac{1}{\chi} \). Thus, parameter \( \frac{1}{\chi} \) can be physically interpreted as the scaling factor. In the range under study, coefficient remains unchanged, so that parameter \( \frac{1}{\chi} \) is also constant.

A variation in the SAW velocity results in a variation in the characteristics of the AO diffraction. For the isotropic Bragg diffraction, a relatively small diffraction angle \( \Theta_1 \) is given by
Hence, the diffraction angle is scaled as $\frac{1}{\chi}$ in the range under study. Therefore, first, the spectrum of spatial frequency is corrected in the same way and, second, an additional mismatch of the wavevectors of the incident and diffracted waves emerges. This leads to a shift of the SAW frequency $f_0$, at which the AO diffraction is realized with the maximum efficiency. Then, a new value of the frequency is written as $f_1 = \chi f_0$. Note that the maximum diffraction efficiency remains unchanged provided that a variation in the overlap integral is neglected.

A minor variation in the diffraction angle affects separation $\Delta s$ of the incident and diffracted beams in the focal plane of a lens. In the approximation of geometrical optics, the following expression is valid: $\Delta s_1 = \frac{1}{\chi} \Delta s_0$, where $\Delta s_1, \Delta s_0$ are the separations with regard to and with neglect of the degradation, respectively.

The working frequency band $\Delta f$ of the AO device is determined by the following main factors: the SAW excitation band and the AO interaction band [5]. For the isotropic Bragg diffraction, the working frequency band is given by the following expression taking into account the spread of the SAW velocities:

$$\Delta f_1 = \frac{2N_{eff} \chi^2 V_0^2 (1 - \Theta_1/4)}{\lambda_0 f_0 W_a} \approx \chi^2 \Delta f_0,$$

where $f_c$ is the central frequency. Neglecting the second term in parentheses in the numerator, we conclude that $\Delta f$ quadratically depends on the SAW velocity fluctuation.

### 5.3 Analysis of the TIAOC characteristics

A variation in the time scale directly affects one of the main parameters of the AO correlator—the maximum delay time $T_A$. In the presence of the SAW velocity fluctuations, this parameter is given by

$$T_{A1} = \frac{W_{opt}}{\chi V_0} = \frac{1}{\chi} T_{A0},$$

where $W_{opt}$ is the optical beam aperture. Note that the scaling laws for $\Delta T_A$ and $T_A$ are identical.

A relative delay $\tau$ of the AO correlator is scaled similarly to $T_A$. One must take into account the time of the SAW propagation from IDT to the AO interaction region, which is similarly scaled:

$$\tau_1 = \frac{\gamma T_{A0}}{\chi} + \frac{L}{\chi V_0} = \frac{1}{\chi} \tau_0,$$

where $\gamma$ is a fraction of $T_A$ and $L$ is the distance between IDT and the AO interaction region.
Based on the analysis of expressions (25) and (26), we draw the following conclusion. In spite of the scaling of parameters $T_A$, $\Delta T_A$ and $\tau$, the range of the relative delays $\Delta \tau$ of the correlator is the same as in the absence of the SAW velocity spread, so that quantity $\gamma$ is not scaled.

The scaling of the working frequency band leads to a variation in the AOTIC base. At a constant integration time, it can be estimated as

$$N_1 = \chi^2 N_0,$$

where $N_1$ and $N_0$ are the AO correlator bases with regard to and with neglect of the SAW velocity spread, respectively.

Consider the effect of a variation in the SAW velocity on the transformation of the correlation signal. For numerical experiments, we employ a mathematical model of the multi-channel TIAOC. Using a mathematical model of the multi-channel TIAOC, one can also numerically analyze the characteristics of a hybrid monochrome TIAOC, in particular, at relatively small SAW variations. The validity of such an approach follows from the comparative analysis of the theoretical and experimental data. We employ an experimental prototype whose structure is described in detail in [16]. The numerical experiments are performed for the wavelength in a vacuum $\lambda_0 = 0.78 \, \mu m$, the initial SAW velocity $V_0 = 3488 \, m/s$, and a rectangular optical aperture function whose value is 7 mm.

To estimate the variation in the shape of the correlation signal in the presence of the SAW velocity fluctuations, we analyze a model scenario in the absence of propagation loss. Such an approach makes it possible to account for the transformations of the correlation signal. Let information signals with equal durations ($T_A$) have a relative delay of 0.5 $T_A$. In this case, the SAW velocity can differ from the calculated value. For the numerical experiments, we choose the same initial data as in the previous case. The optical aperture function and all of the signals applied to the device have rectangular shapes.

Figure 13 demonstrates the results of the computer simulation. At the first stage, when the SAW velocity coincides with the calculated velocity, a classical correlation signal in the image plane represents an almost equilateral triangle. When the SAW velocity decreases, the shape of this signal is varied. In the case under study, a simultaneous shrinkage of the left- and right-hand wings of the correlation signals leads to its narrowing. This is due to the spatial compression of the acoustic signal, which is proportional to a variation in the SAW velocity. However, in all of the transformations, the correlation peak amplitude remains unchanged. The reason for this lies in the dependence of this amplitude on the integration time, which remains constant ($T_A$). The following conclusion can be drawn from the simulation results. The expression that can be used to estimate the narrowing of the correlation signal in the above range of a decrease in the SAW velocity is written as

$$W_{cor_1} = \chi W_{cor_0},$$

where $W_{cor_1}$ and $W_{cor_0}$ are the apertures (widths) of the correlation signal with regard to and neglect of a decrease in the SAW velocity, respectively.

An increase in the SAW velocity leads to a substantially different transformation of the correlation signal: it becomes asymmetric. In the case under study, a decrease in the left-hand wing is accompanied by an increase in the right-hand wing. This is due to the spatial extension of the acoustic signal, which is proportional to the variation in the SAW velocity.
Fig. 13. Normalized correlation signal ($J_p$, norm) in the TIAOC image plane with regard to the SAW velocity fluctuations for an input signal duration of $T_A$ and a relative delay of $0.5T_A$ at $\chi = (1) 1.2$, (2) 0.9, and (3) 1.1

The maximum amplitude of the correlation peak linearly decreases with an increasing parameter $\chi$.

A similar analysis can be performed for other pulse durations and the corresponding integration times. It follows from the calculated results that a decrease in the pulse duration causes transformations of the correlation signal that are similar to the above transformations.

In a real device, we must take into account the variation in the delay in the acoustic path. As mentioned, this leads to a variation in the relative delay of the signals. To eliminate the effect of the acoustic delay, we consider a general case in which the relative delay is varied in the entire allowed range $0$–$T_A$. It follows from [23] that the correlation peak height exhibits an approximately parabolic decrease in the absence of the SAW velocity degradation. Using a similar approach, we generalize the simulated results on the case of the spread of the SAW velocities. Figure 14 shows the results of the analysis. It is seen that a decrease in the SAW velocity causes a symmetric decrease in the correlation peak. Opposite results are obtained when the SAW velocity increases. A sharper decrease in the correlation...
Fig. 14. Plots of the normalized correlation peak height ($J_p$, norm) vs. relative delay $\gamma$ (in fractions of $T_A$) for input pulses with a duration of $T_A$ with regard to the SAW velocity fluctuations at $\chi = (1) 1.2$, $(2) 0.9$, and $(3) 1.1$

peak height is observed at $\gamma < 0.5 \ T_A$, whereas the peak height starts increasing (in comparison with the ideal scenario) at $\gamma > 0.5 \ T_A$. Note that, at $\gamma > 0.8 \ T_A$, the peak height becomes higher than that in the ideal case. Such a character of this dependence is realized at any variations in the SAW velocity in the range under study.

5.4 Analysis of the AOSA characteristics

We analyze the manifestation of a minor variation in the SAW velocity in the output characteristics of the broadband AOSA. For this purpose, we employ the experimentally verified mathematical model of this device from [5]. By analogy with the above analysis, we choose the experimental device whose structure is described in detail in [16]. For the numerical calculations, we assume that the WAOC contains WBAOC with a complicated ITD system, integrating lens, and incoupling and outcoupling optical prisms. The remaining initial data correspond to the experimental device from [16]. The aplanatic lenses for the WAOC are manufactured using the TIPE technology [19]. We assume that the optical aperture function exhibits a nearly Gaussian shape with the width $W_{opt} = 5$ mm. Using these parameters, we perform computer simulation to optimize the interdigitated structure, which is needed to realize the maximum band of the analyzed radio frequencies, and to optimize the topology of the WAOC lens system, which is needed for the maximum optical resolution with the technique from [5].
Note several features of the realization of the broadband AO diffraction by the synthesized acoustic field. These are related to the differences of the overlap integral, interference phenomena, and acoustic loss at low and high frequencies. To estimate the variation in the working frequency band related to the SAW velocity fluctuations, we analyze two WBAOC modifications. Each cell contains three IDT structures that generate an acoustic field with crossed beams. The first cell is constructed for the frequency range 0.3–0.7 GHz. The second cell works in the frequency range 0.7–1.3 GHz. The experimental and theoretical parameters and frequency characteristics of the cells can be found in [23].

Figure 15 shows the simulated diffraction characteristics of both cells in the presence of the SAW velocity fluctuations: plots of the normalized working frequency band (at a level of −3 dB) and the diffraction efficiency at the critical frequency (nonuniformity of the frequency response), where the highest sensitivity to the SAW velocity variations is realized, vs. parameter \( \chi \). For the first and second cells, the critical frequencies are 567 and 1010 MHz, respectively. The analysis of the simulated results makes it possible to reach the following conclusions. The scaling of the working frequency band in the range of relatively small variations in the SAW velocity linearly depends on parameter \( \chi \). The slope of this curve for the high-frequency cell 2 is higher than that for the low-frequency cell 1. An increase in the nonuniformity of the frequency response is related to a violation of the phase relationships [5]. Note its developed frequency dependence. To determine the level of the effect of the mechanism under study at which the allowed level (e.g., −3 dB) is exceeded, a detailed simulation is needed in each specific case.

Fig. 15. Plots of (a) the normalized working frequency band (\( \Delta f, \text{norm} \)) and (b) diffraction efficiency \( D \) at the critical frequency vs. SAW velocity fluctuation coefficient for (1) the first and (2) second cells.
The SAW velocity fluctuation also causes a variation in the WAOC frequency resolution. It follows from the numerically calculated distributions of the optical intensity at the focal plane of the integrating lens that, for the processing of two RF signals with allowance for a 10% variation in the SAW velocity, the resolution is virtually inversely proportional to parameter $\chi$ (Fig. 16). Note that, in the ideal case, the frequency resolution is 2 MHz.

Based on the simulated results for the working frequency band and the resolution, we conclude that the number of points of the broadband AOSA remains almost unchanged in the low-frequency range in the presence of SAW velocity fluctuations.

Fig. 16. Plot of the AOSA normalized frequency resolution ($R_f$, norm) vs. SAW velocity fluctuation coefficient

5.5 Conclusion

The characteristics of two basic AO devices (time-integrating correlator and broadband spectrum analyzer of radio signals) are theoretically analyzed and numerically studied in the presence of SAW velocity fluctuations. The devices are based on a waveguide AO chip that is fabricated at a Y-cut lithium niobate substrate. In the analyzed range of the SAW velocity fluctuations, the SAW velocity linearly depends on the level of the degradation factor. This causes the scaling of the characteristics of the device. Several parameters (Bragg diffraction angle, separation of optical beams, maximum delay time, range of delay times, relative delay, and frequency resolution) are scaled with a coefficient that is equal to the inverse relative variation in the SAW velocity. For the narrowband and broadband scenarios, the working frequency band exhibits quadratic and linear scalings, respectively.
The correlator base is quadratically scaled, and the number of points of the spectrum analyzer remains almost unchanged. The correlation peak height exhibits complicated variations in the presence of the SAW velocity fluctuations. The range of the correlator relative delays is not scaled.

6. Conclusions

The newly developed methods for real time data processing are proposed. To increase the efficiency of the methods we must use and a proposed make it possible to process both a synthesized optical aperture and a synthesized acoustic aperture. The mathematical models of the units whose acousto-optic chip is based on the Y-cut lithium niobate substrate are developed. We theoretically and numerically analyzed the unit characteristics under design and technology conditions. The results obtained can be used for the practical elaboration of the high efficiency AO devices.

7. Acknowledgments


8. References

SAW devices are widely used in multitude of device concepts mainly in MEMS and communication electronics. As such, SAW based micro sensors, actuators and communication electronic devices are well known applications of SAW technology. For example, SAW based passive micro sensors are capable of measuring physical properties such as temperature, pressure, variation in chemical properties, and SAW based communication devices perform a range of signal processing functions, such as delay lines, filters, resonators, pulse compressors, and convolvers. In recent decades, SAW based low-powered actuators and microfluidic devices have significantly added a new dimension to SAW technology. This book consists of 20 exciting chapters composed by researchers and engineers active in the field of SAW technology, biomedical and other related engineering disciplines. The topics range from basic SAW theory, materials and phenomena to advanced applications such as sensors actuators, and communication systems. As such, in addition to theoretical analysis and numerical modelling such as Finite Element Modelling (FEM) and Finite Difference Methods (FDM) of SAW devices, SAW based actuators and micro motors, and SAW based micro sensors are some of the exciting applications presented in this book. This collection of up-to-date information and research outcomes on SAW technology will be of great interest, not only to all those working in SAW based technology, but also to many more who stand to benefit from an insight into the rich opportunities that this technology has to offer, especially to develop advanced, low-powered biomedical implants and passive communication devices.

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